Problem 1 Let oracle $\mathcal{X}$ be an oracle that, on input $x$, returns a random integer in [1..10] other than $x$. Let $\mathcal{Y}$ be an oracle that, on input $x$, returns a random integer in [1..10]. Define the advantage of an adversary $A$ is as $\operatorname{Adv}(A)=\operatorname{Pr}\left[A^{\mathcal{X}}=1\right]-\operatorname{Pr}\left[A^{\mathcal{Y}}=1\right]$. For each $q \geq 0$ define an adversary $A_{q}$ that achieves maximal advantage. Compute the advantage of adversary $A_{100}$.

Problem 2 Fix an encryption scheme $\Pi=(\mathcal{E}, \mathcal{K}, \mathcal{D})$. Let $M_{1}, \ldots, M_{10}$ be fixed messages. Suppose you have an efficient adversary $A$ that, given $C_{1}, \ldots, C_{10}, C$ determined by $C_{i} \stackrel{\&}{\leftarrow} \mathcal{E}_{K}\left(M_{i}\right), M \stackrel{\S}{\leftarrow}\{0,1\}^{8}, C \stackrel{\&}{\leftarrow} \mathcal{E}_{K}(M)$, has an $10 \%$ chance to compute $M$. Describe an efficient adversary $B$ that attacks $\Pi$ and lower bound its advantage (in the indsense).

Problem 3 Consider the following block cipher $E:\{0,1\}^{3} \times\{0,1\}^{2} \rightarrow\{0,1\}^{2}$ :

| key | 0 | 1 | 2 | 3 |
| :---: | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 2 | 3 |
| 1 | 3 | 0 | 1 | 2 |
| 2 | 2 | 3 | 0 | 1 |
| 3 | 1 | 2 | 3 | 0 |
| 4 | 0 | 3 | 2 | 1 |
| 5 | 1 | 0 | 3 | 2 |
| 6 | 2 | 1 | 0 | 3 |
| 7 | 3 | 2 | 1 | 0 |

(The eight possible keys are the eight rows, and each row shows where points 0,1 , 2 , and 3 map to.) Compute the maximal advantage an adversary can get, in the prp-sense, if $A$ uses (a) one query, (b) two queries, and (c) four queries. Justify your answers.

