COMP 754 — Cryptography & Security — Aj. Phillip Rogaway Problem Set #3 — Out: 1 Aug 02 — Due: 13 Aug 02 (in class)

- **Problem 1** Let oracle  $\mathcal{X}$  be an oracle that, on input x, returns a random integer in [1..10] other than x. Let  $\mathcal{Y}$  be an oracle that, on input x, returns a random integer in [1..10]. Define the advantage of an adversary A is as  $\mathbf{Adv}(A) = \Pr[A^{\mathcal{X}} = 1] \Pr[A^{\mathcal{Y}} = 1]$ . For each  $q \geq 0$  define an adversary  $A_q$  that achieves maximal advantage. Compute the advantage of adversary  $A_{100}$ .
- **Problem 2** Fix an encryption scheme  $\Pi = (\mathcal{E}, \mathcal{K}, \mathcal{D})$ . Let  $M_1, \ldots, M_{10}$  be fixed messages. Suppose you have an efficient adversary A that, given  $C_1, \ldots, C_{10}, C$  determined by  $C_i \stackrel{\$}{\leftarrow} \mathcal{E}_K(M_i), M \stackrel{\$}{\leftarrow} \{0, 1\}^8, C \stackrel{\$}{\leftarrow} \mathcal{E}_K(M)$ , has an 10% chance to compute M. Describe an efficient adversary B that attacks  $\Pi$  and lower bound its advantage (in the ind-sense).

**Problem 3** Consider the following block cipher  $E: \{0,1\}^3 \times \{0,1\}^2 \rightarrow \{0,1\}^2$ :

key	0	1	2	3
0	0	1	2	3
1	3	0	1	2
2	2	3	0	1
3	1	2	3	0
4	0	3	2	1
5	1	0	3	2
6	2	1	0	3
7	3	2	1	0

(The eight possible keys are the eight rows, and each row shows where points 0, 1, 2, and 3 map to.) Compute the maximal advantage an adversary can get, in the prp-sense, if A uses (a) one query, (b) two queries, and (c) four queries. Justify your answers.