CS Preliminaries

Computer Science

- Computational solutions to problems: algorithms
- Programming the solutions: programs
- Data storage and access: databases
- Data Analysis: for hypothesis generation and testing
- Human-computer Interfaces: interaction with data
- Building systems: hardware and software
- Education

What is a solution to a problem: an algorithm

- A procedure designed to perform a certain task, or solve a particular problem
- Algorithms are recipes: ordered lists of steps to follow in order to complete a task
- Abstract idea behind particular implementation in a computer program

1. Algorithms in Bioinformatics

Theoretical Computer Scientists are contributors to the genomic revolution

- Sequence comparison
- Genome Assembly
- Phylogenetic Trees
- Microarray design (SBH)
- Data Integration
- Gene network inference

Algorithm Design

- Recognize the structure of a given problem:
 - Where does it come from?
 - What does it remind of?
 - How does it relate to established problems?
- Build on existing, efficient data structures and algorithms to solve the problem
- If the problem is difficult to solve efficiently, use approximative algorithms

Problems and Solutions

In algorithmic lingo:

- <u>Problems</u> are very specific, general mathematical tasks, that take variables as input and yield variables as output.
- Particularizations (assigning values to the variables) are called <u>instances</u>.
- <u>Problem</u>: Multiply(a,b): Given integers a and b, compute their product a*b.
- <u>Instance</u>: Multiply (13, 243).

Algorithms produce solutions for any given instance of a general problem

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Multiply(a,b):
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0) Let Product = 0

1) Take the k-th rightmost digit of b and multiply a by it. Attach k-1 zeros to the right, and add to Product.

- 2) Repeat Step 1. for all digits of b.
- 3) Product = a*b

Multiply (13, 243) = 3159

Algorithm Analysis

Correctness

- Exact solutions require a proof of correctness
- Heuristics: approximate solutions
- Resource Efficiency (complexity)
 - Time: number of steps to follow to obtain a solution as a function of the input size
 - Space: amount of memory required for the algorithm execution
- Best, Average, and Worst Case Analysis

Time / Space Complexity

- Input size: how many units of constant size does it take to represent the input? This is dependent on the <u>computational model</u>, but can be thought of as the storage size of the input. The input size is usually n.
- Running time: f(n) = const., n, log n, Poly(n), eⁿ

Big Oh Notation

 Asymptotic upper bound on the number of steps an algorithm takes (in the worst case)

- f(n) = O(g(n)) iff there is a constant c such that for all large n, 0 <= f(n) <= c*g(n)
- More intuitively: f(n) is almost always less than or equal to g(n), i.e. algorithm with t.c. f(n) will almost never take more time than one with t.c. of g(n)

Big Oh, examples

- Const. = O(1)
- 3n = O(n)
- $3n = O(n^2)$
- $\log n = O(n)$
- $Poly(n) = O(e^n)$
- O(n) time algorithm is called linear
- O(Poly(n)) is polynomial
- O(eⁿ) is polynomial

Basic Complexity Theory

- Classification of Problems based on the time/space complexity of their solutions
- Class P: Problems with polynomial time algorithms t.c. = O(Poly(n))
- Class NP: (non-deterministic polynomial) Problems whose solution instances can be verified in Poly(n) time.

Complexity, contd.

- NP-complete problems: a polynomial algorithm for one of them would mean all problems in NP are polynomial time
- But, NO polynomial time algorithms for NP problems are known
- P ≠ NP? Still unsolved, although strongly suspected true.
- NP complete problems: 3-SAT, Hamiltonian Cycle, Vertex Cover, Maximal Clique, etc. Thousands of NP-complete problems known
- Compendium:

http://www.nada.kth.se/~viggo/problemlist/compendium.html

Why All That?

- Many important problems in the real world tend to be NP-complete
- That means exact solutions are intractable, but for very small instances
- Proving a problem to be NP-complete is just a first step: a good algorist would use good and efficient heuristics

Popular Algorithms

- Sorting
- String Matching
- Graph Algorithms
 - Graph representation: linked lists, incidence matrix
 - Graph Traversal (Depth First and Breadth First)
 - Minimum Spanning Trees
 - Shortest Paths
- Linear Programming

Algorithmic Techniques

Combinatorial Optimization Problems

 Find min (max) of a given function under given

constraints

- <u>Greedy</u> best solution locally
- <u>Dynamic Programming</u> best global solution, if the problem has a nice structure
- <u>Simulated Annealing</u>: if not much is known about the problem. Good general technique

Data Structures

- Once a given problem is digested, algorithm design becomes an engineering discipline: having a big toolbox and matching the tools to the task at hand
- A major part of the toolbox are <u>data</u> <u>structures:</u>

Data representations allowing efficient performance of basic operations

Basic Opperations

• Store/Search:

- Search(x)
- Delete(x)
- Insert(x)
- Priority:
 - FindMIN
 - FindMAX
- Set:
 - UnionSet
 - FindElement

Basic Data Structures

- Static: arrays and matrices
 - Array of n elements: a[i], 0 <= i <= n-1</p>

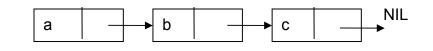
1	2	3	4	5
a[1]	a[2]	a[3]	a[4]	a[5]

- Matrix of n*n elements:
 m[i][j], 0 <= i, j <= n-1
- Basic operations are O(1)

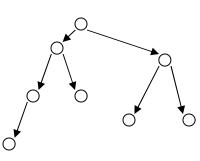
	1	2	3	4
1	m[1][1]	m[1][2]	m[1][3]	m[1][4]
2	m[2][1]	m[2][2]	m[2][3]	m[2][3]
3	m[3][1]	m[3][2]	m[3][3]	m[3][4]

Dynamic Data Structures: linked lists, trees and balanced trees, hash tables

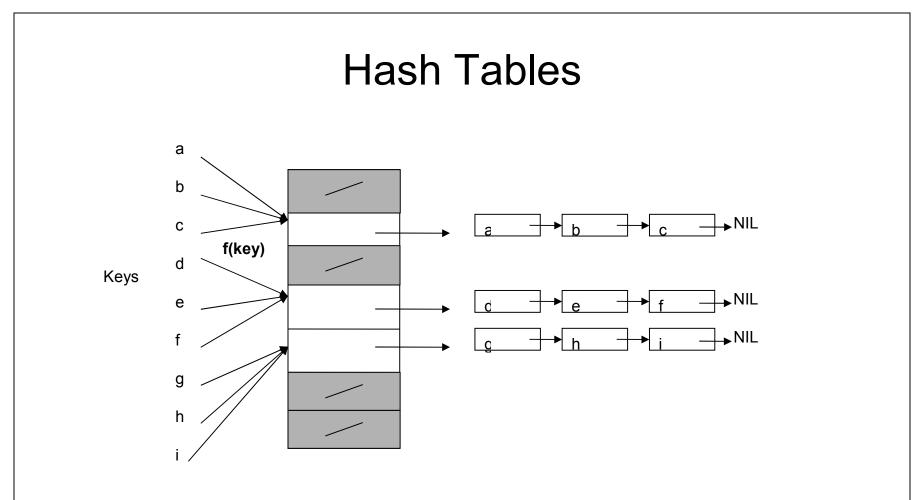
- No static memory allocation: items are added/deleted on the go
- Linked Lists (basic operations are O(n)):



Trees



Balanced tree: Height is O(logn). Basic operations are O(log n)



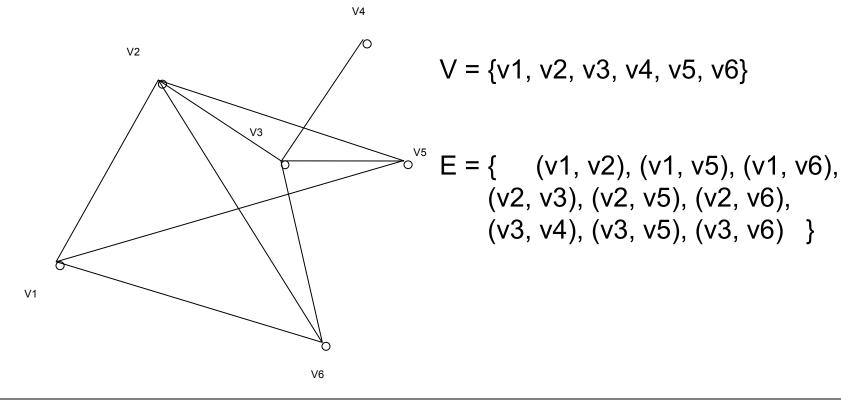
A good hash function f(key) yields constant search time O(1).

Set Data Structures

- Given sets A={1,2,3,4} and B={1,3}
- Operations: Find, Union
- Example:
 - -Find(A,3) = yes
 - Find(A,5) = no
 - -Find(B,3) = yes
 - Union(A,B) = {1,2,3,4}
- Very efficient: almost linear in the number of union+find operations

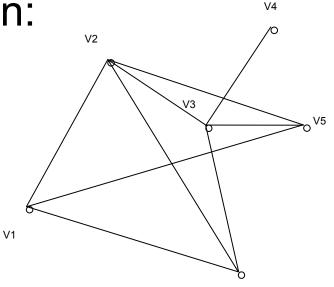
Graphs

 Graph G(V, E). V is a set of vertices, E a set of edges



• Linked list representation:

v1: v2, v5, v6 v2: v1, v3, v5, v6 v3: v2, v4, v5, v6 v4: v3 v5: v1, v2, v3 v6: v1, v2, v3



- V6
- Adjacency Matrix Representation

	V1	V2	V3	V4	V5	V6
V1		1	0	0	1	1
V2	1		1	0	1	1
V3	0	1		1	1	1
V4	0	0	1		0	0
V5	1	1	1	0		0
V6	1	1	1	0	0	

A Greedy Clustering Example

• Clustering is a very important tool in analysis of large quantities of data

 Clustering: Given a number of objects we want to group them based on similarity

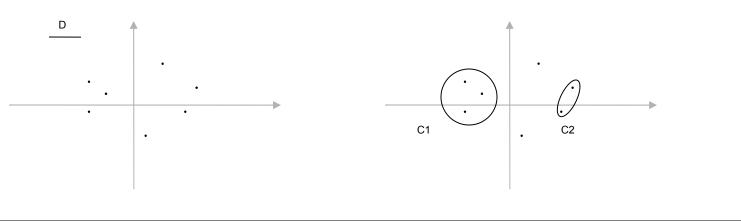
 Here we will work out a very simple example: clustering points in a plane by single-link hierarchical clustering

Clustering Points in the Plane

Problem 1: Given *n* points $p_1(x_1, y_1), p_2(x_2, y_2), ..., p_n(x_n, y_n)$

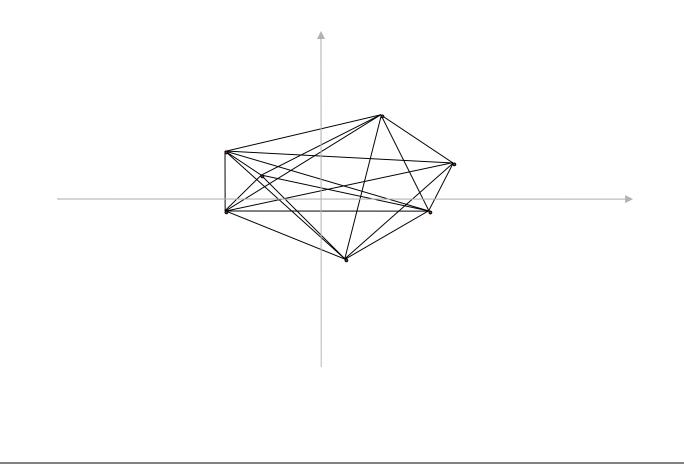
in a plane, cluster them so that if the distance between two points is less than D they are in the same cluster

Input: D, $p_1(x_1, y_1), p_2(x_2, y_2), \dots, p_n(x_n, y_n)$ **Output:** Sets (clusters) of points C₁, C₂, ..., C_k.

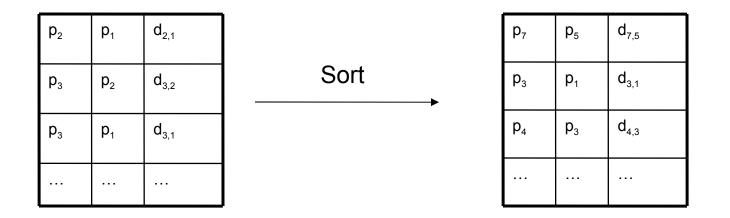


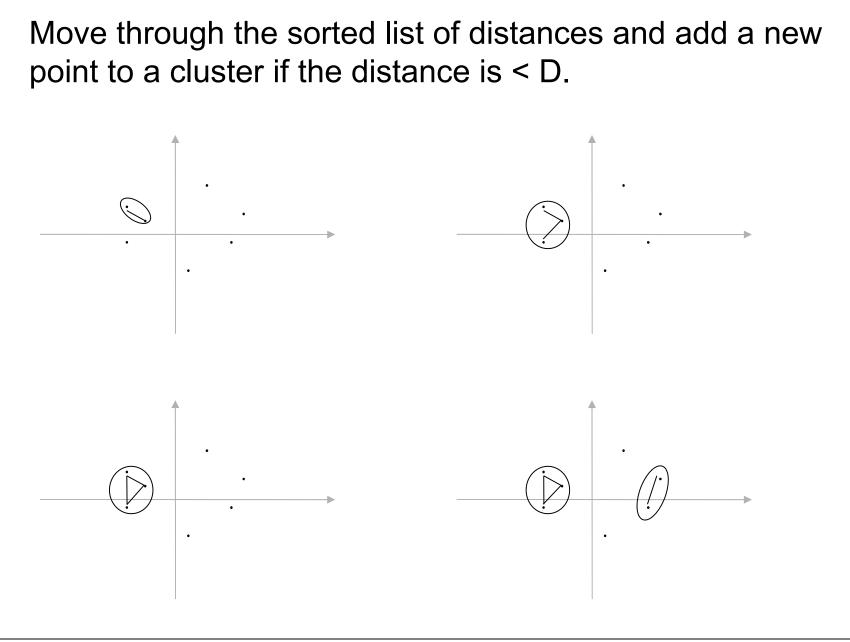
Algorithm Draft

Calculate distances between point pairs



• Sort the distances in ascending order





Algorithm in Detail

Data Structure for the graph: adjacency matrix

р ₂	p ₁	d _{2,1}
p ₃	p ₂	d _{3,2}
p ₃	p ₁	d _{3,1}

 Data Structure for the clusters: Set (Union / Find)

Algorithm in detail

- Calculate distances O(n²)
 For all pairs i,j calculate d(i,j)
- Sort adjacency table O(n² log n)
- Start with n sets, p₁,p₂,...,p_n. Build a linkedlist representation of a graph:
 - Get the next smallest distance, d(i,j)
 - If d(i,j) >= D done
 - Else Union(Find(p_i),Find(p_j))
- Traverse the graph to find the <u>connected</u> <u>components (DFS)</u>

Algorithm Analysis

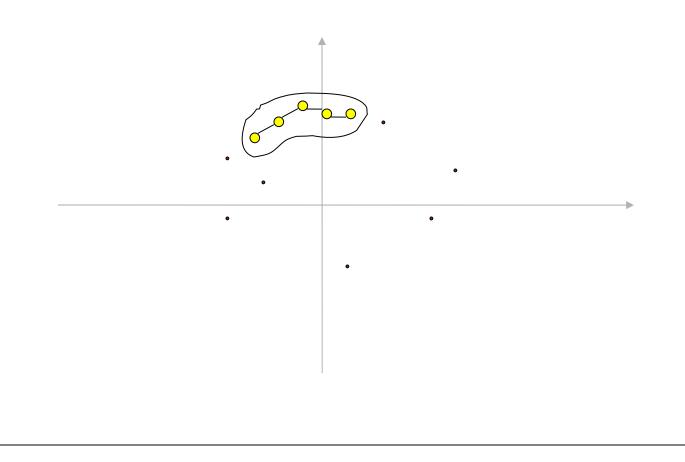
- Correctness:
 - All distances less than D are added
 - Clusters contain all points with distance < D to some other point in the cluster
- Time complexity:
 - Bounded above by the sorting step $-O(n^2 \log n)$

Discussion

- This algorithm is known as Single-Link Hierarchical Clustering
- It is a version of Kruskal's Minimum Spanning Tree Algorithm
- It is fast

Performance on Real Data

• Lousy: Chaining effects



Better Approaches: Complete-Link Clustering Problem 2: Given *n* points $p_1(x_1, y_1), p_2(x_2, y_2), ..., p_n(x_n, y_n)$ in a plane, cluster them so that the distance between any two points in a cluster is less than D **Input:** D, $p_1(x_1, y_1), p_2(x_2, y_2), \dots, p_n(x_n, y_n)$ **Output:** Sets (clusters) of points $C_1, C_2, ..., C_k$.

2. Bio-databases

- A biological database is a large, organized body of persistent data, usually associated with computerized software designed to update, query, and retrieve components of the data stored within the system.
 - easy access to the information
 - a method for extracting only that information needed to answer a specific biological question
- Many databases are linked through a unique search and retrieval system, eg NCBI's Entrez.

Database Interfacing

- APIs: scripts in Perl, Python, R
- Direct online:
 - NCBI entrez
 - KEGG
 - Reactome
 - -etc.

3. Workflows

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