ECS 165B: Database System Implementation
Lecture 8

UC Davis
April 14, 2011

Acknowledgements: portions based on slides by Raghu Ramakrishnan and Johannes Gehrke.
Class Agenda

• Last time:
  – Intro to database theory, cont’d: containment, equivalence, and minimization of conjunctive queries

• Today:
  – Overview of indexing

• Reading
  – Chapter 14
Announcements

Project Part 1 due Sunday @ 11:59pm

- submit.sh early, submit.sh often

Office hours today (055 Kemper): TJ 10am-12pm, Armen 1pm-3pm

Have you done an svn commit lately?

- group9: garysu, yexeric
- group10: trdelgad, tadileo
- group13: kssassen
- group14: mtgarip, youchen
Overview of Indexing
Indexes

• An *index* on a file speeds up selections on the *search key fields* for the index.
  – Any subset of the fields of a relation can be the search key for an index on the relation.
  – *Search key* is not the same as *key* (minimal set of fields that uniquely identify a record in a relation).

• An index contains a collection of *data entries*, and supports efficient retrieval of all data entries $k^*$ with a given key value $k$. 
Alternatives for Data Entry $k^*$ in Index

• Three alternatives:
  – Data record with key value $k$
  – $<k, \text{rid of data record with search key value } k>$
  – $<k, \text{list of rids of data records with search key } k>$

• Choice of alternative for data entries is orthogonal to the indexing technique used to locate data entries with a given key value $k$.
  – Examples of indexing techniques: B+ trees, hash-based structures
  – Typically, index contains auxiliary information that directs searches to the desired data entries
Alternatives for Data Entries (Contd.)

- **Alternative 1:**
  - If this is used, index structure is a file organization for data records (instead of an unordered heap file or sorted file).
  - At most one index on a given collection of data records can use Alternative 1. (Otherwise, data records are duplicated, leading to redundant storage and potential inconsistency.)
  - If data records are very large, # of pages containing data entries is high. Implies size of auxiliary information in the index is also large, typically.
Alternatives for Data Entries (Contd.)

• Alternatives 2 and 3:
  
  - Data entries typically much smaller than data records. So, better than Alternative 1 with large data records, especially if search keys are small. (Portion of index structure used to direct search, which depends on size of data entries, is much smaller than with Alternative 1.)

  - Alternative 3 more compact than Alternative 2, but leads to variable sized data entries even if search keys are of fixed length.
Index Classification

• **Primary vs. secondary:** If search key contains primary key, then called primary index.
  – *Unique* index: Search key contains a candidate key.

• **Clustered vs. unclustered:** If order of data records is the same as, or `close to`, order of data entries, then called clustered index.
  – Alternative 1 implies clustered; in practice, clustered also implies Alternative 1 (since sorted files are rare).
  – A file can be clustered on at most one search key.
  – Cost of retrieving data records through index varies *greatly* based on whether index is clustered or not!
Clustered vs. Unclustered Index

• Suppose that Alternative (2) is used for data entries, and that the data records are stored in a Heap file.
  – To build clustered index, first sort the Heap file (with some free space on each page for future inserts).
  – Overflow pages may be needed for inserts. (Thus, order of data recs is `close to’, but not identical to, the sort order.)
Hash-Based Indexes

• Good for equality selections.
  • Index is a collection of buckets. Bucket = primary page plus zero or more overflow pages.
  • Hashing function \( h \): \( h(r) = \) bucket in which record \( r \) belongs. \( h \) looks at the search key fields of \( r \).

• If Alternative (1) is used, the buckets contain the data records; otherwise, they contain \(<\text{key, rid}>\) or \(<\text{key, rid-list}>\) pairs.
Leaf pages contain *data entries*, and are chained (prev & next).
Non-leaf pages contain *index entries* and direct searches:
Example B+ Tree

- Find 28*? 29*? All > 15* and < 30*
- Insert/delete: Find data entry in leaf, then change it. Need to adjust parent sometimes.
  - And change sometimes bubbles up the tree
Cost Model for Our Analysis

We ignore CPU costs, for simplicity:

- **B**: The number of data pages
- **R**: Number of records per page
- **D**: (Average) time to read or write disk page
- Measuring number of page I/O’s ignores gains of pre-fetching a sequence of pages; thus, even I/O cost is only approximated.
- Average-case analysis; based on several simplistic assumptions.

☞ Good enough to show the overall trends!
Comparing File Organizations

- Heap files (random order; insert at eof)
- Sorted files, sorted on $<age, sal>$
- Clustered B+ tree file, Alternative (1), search key $<age, sal>$
- Heap file with unclustered B + tree index on search key $<age, sal>$
- Heap file with unclustered hash index on search key $<age, sal>$
Operations to Compare

- Scan: Fetch all records from disk
- Equality search
- Range selection
- Insert a record
- Delete a record
Assumptions in Our Analysis

• Heap Files:
  – Equality selection on key; exactly one match.

• Sorted Files:
  – Files compacted after deletions.

• Indexes:
  – Alt (2), (3): data entry size = 10% size of record
  – Hash: No overflow buckets.
    • 80% page occupancy => File size = 1.25 data size
  – Tree: 67% occupancy (this is typical).
    • Implies file size = 1.5 data size
### Cost of Operations

<table>
<thead>
<tr>
<th></th>
<th>(a) Scan</th>
<th>(b) Equality</th>
<th>(c) Range</th>
<th>(d) Insert</th>
<th>(e) Delete</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1) Heap</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(2) Sorted</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(3) Clustered</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(4) Unclustered</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Tree index</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(5) Unclustered</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hash index</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Several assumptions underlie these (rough) estimates!
## Cost of Operations

<table>
<thead>
<tr>
<th></th>
<th>(a) Scan</th>
<th>(b) Equality</th>
<th>(c) Range</th>
<th>(d) Insert</th>
<th>(e) Delete</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>(1) Heap</strong></td>
<td>BD</td>
<td>0.5BD</td>
<td>BD</td>
<td>2D</td>
<td>Search +D</td>
</tr>
<tr>
<td><strong>(2) Sorted</strong></td>
<td>BD</td>
<td>Dlog₂B</td>
<td>Dlog₂B + # matches</td>
<td></td>
<td>Search + BD</td>
</tr>
<tr>
<td><strong>(3) Clustered</strong></td>
<td>1.5BD</td>
<td>Dlog₂ 1.5B</td>
<td>Dlog₂ 1.5B + # matches</td>
<td>Search + BD</td>
<td>Search + BD</td>
</tr>
<tr>
<td><strong>(4) Unclustered Tree index</strong></td>
<td>BD(R+0.15)</td>
<td>D(1 + log₂ 0.15B)</td>
<td>Dlog₂ 0.15B + # matches</td>
<td>D(3 + log₂ 0.15B)</td>
<td>Search + 2D</td>
</tr>
<tr>
<td><strong>(5) Unclustered Hash index</strong></td>
<td>BD(R+0.125)</td>
<td>2D</td>
<td>BD</td>
<td>4D</td>
<td>Search + 2D</td>
</tr>
</tbody>
</table>

*Several assumptions underlie these (rough) estimates!*
Understanding the Workload

• For each query in the workload:
  – Which relations does it access?
  – Which attributes are retrieved?
  – Which attributes are involved in selection/join conditions? How selective are these conditions likely to be?

• For each update in the workload:
  – Which attributes are involved in selection/join conditions? How selective are these conditions likely to be?
  – The type of update (INSERT/DELETE/UPDATE), and the attributes that are affected.
Choice of Indexes

• What indexes should we create?
  – Which relations should have indexes? What field(s) should be the search key? Should we build several indexes?

• For each index, what kind of an index should it be?
  – Clustered? Hash/tree?
Choice of Indexes (Contd.)

• **One approach:** Consider the most important queries in turn. Consider the best plan using the current indexes, and see if a better plan is possible with an additional index. If so, create it.
  – Obviously, this implies that we must understand how a DBMS evaluates queries and creates *query evaluation plans!*
  – For now, we discuss simple 1-table queries.

• Before creating an index, must also consider the impact on updates in the workload!
  – **Trade-off:** Indexes can make queries go faster, updates slower. Require disk space, too.
Index Selection Guidelines

• Attributes in WHERE clause are candidates for index keys.
  – Exact match condition suggests hash index.
  – Range query suggests tree index.
    • Clustering is especially useful for range queries; can also help on equality queries if there are many duplicates.

• Multi-attribute search keys should be considered when a WHERE clause contains several conditions.
  – Order of attributes is important for range queries.
  – Such indexes can sometimes enable index-only strategies for important queries.
    • For index-only strategies, clustering is not important!

• Try to choose indexes that benefit as many queries as possible. Since only one index can be clustered per relation, choose it based on important queries that would benefit the most from clustering.
Examples of Clustered Indexes

• B+ tree index on E.age can be used to get qualifying tuples.
  – How selective is the condition?
  – Is the index clustered?

• Consider the GROUP BY query.
  – If many tuples have \( E.age > 10 \), using \( E.age \) index and sorting the retrieved tuples may be costly.
  – Clustered \( E.dno \) index may be better!

• Equality queries and duplicates:
  – Clustering on \( E.hobby \) helps!

SELECT E.dno
FROM Emp E
WHERE E.age>40

SELECT E.dno, COUNT (*)
FROM Emp E
WHERE E.age>10
GROUP BY E.dno

SELECT E.dno
FROM Emp E
WHERE E.hobby=Stamps
Indexes with Composite Search Keys

• **Composite Search Keys:** Search on a combination of fields.
  
  – **Equality query:** Every field value is equal to a constant value. E.g. wrt <sal,age> index:
    
    • age=20 and sal=75
  
  – **Range query:** Some field value is not a constant. E.g.:
    
    • age=20; or age=20 and sal > 10

• Data entries in index sorted by search key to support range queries.
  
  – Lexicographic order, or
  
  – Spatial order.

Examples of composite key indexes using lexicographic order.

Data records sorted by name

Data entries in index sorted by <sal,age>

Data entries sorted by <sal>
Composite Search Keys

• To retrieve Emp records with $age=30$ AND $sal=4000$, an index on $<age,sal>$ would be better than an index on $age$ or an index on $sal$.
  – Choice of index key orthogonal to clustering etc.

• If condition is: $20<age<30$ AND $3000<sal<5000$:
  – Clustered tree index on $<age,sal>$ or $<sal,age>$ is best.

• If condition is: $age=30$ AND $3000<sal<5000$:
  – Clustered $<age,sal>$ index much better than $<sal,age>$ index!

• Composite indexes are larger, updated more often.
Index-Only Plans

- A number of queries can be answered without retrieving any tuples from one or more of the relations involved if a suitable index is available.

```
SELECT D.mgr
FROM Dept D, Emp E
WHERE D.dno=E.dno

SELECT D.mgr, E.eid
FROM Dept D, Emp E
WHERE D.dno=E.dno

SELECT E.dno, COUNT(*)
FROM Emp E
GROUP BY E.dno

SELECT E.dno, MIN(E.sal)
FROM Emp E
GROUP BY E.dno

SELECT AVG(E.sal)
FROM Emp E
WHERE E.age=25 AND E.sal BETWEEN 3000 AND 5000
```
Index-Only Plans (Contd.)

• Index-only plans are possible if the key is <dno,age> or we have a tree index with key <age,dno>
  – Which is better?
  – What if we consider the second query?

SELECT E.dno, COUNT (*)
FROM Emp E
WHERE E.age=30
GROUP BY E.dno

SELECT E.dno, COUNT (*)
FROM Emp E
WHERE E.age>30
GROUP BY E.dno
Summary (Contd.)

• Index is a collection of data entries plus a way to quickly find entries with given key values. Data entries can be actual data records, \(<\text{key}, \text{rid}>\) pairs, or \(<\text{key}, \text{rid-list}>\) pairs.
  – Choice orthogonal to *indexing technique* used to locate data entries with a given key value.

• Can have several indexes on a given file of data records, each with a different search key.

• Indexes can be classified as clustered vs. unclustered, primary vs. secondary, and dense vs. sparse. Differences have important consequences for utility/performance.
Summary (Contd.)

• Understanding the nature of the *workload* for the application, and the performance goals, is essential to developing a good design.
  – What are the important queries and updates? What attributes/relations are involved?

• Indexes must be chosen to speed up important queries (and perhaps some updates!).
  – Index maintenance overhead on updates to key fields.
  – Choose indexes that can help many queries, if possible.
  – Build indexes to support index-only strategies.
  – Clustering is an important decision; only one index on a given relation can be clustered!
  – Order of fields in composite index key can be important.