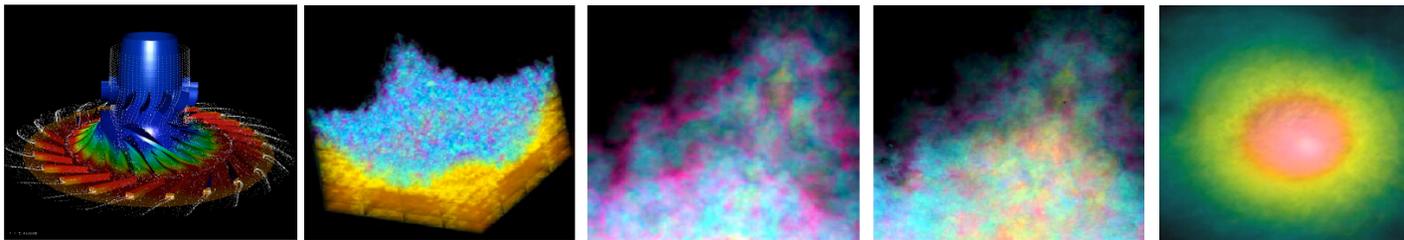
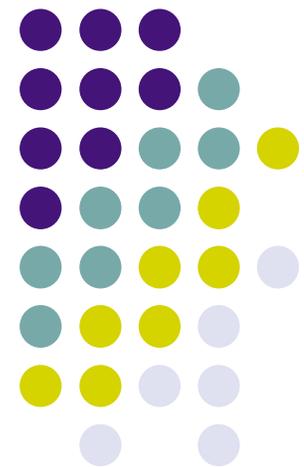


# Navigating Large Scale Scalar Volumes

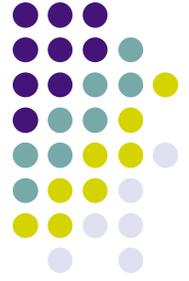


Han-Wei Shen

Department of Computer Science and Engineering  
The Ohio State University

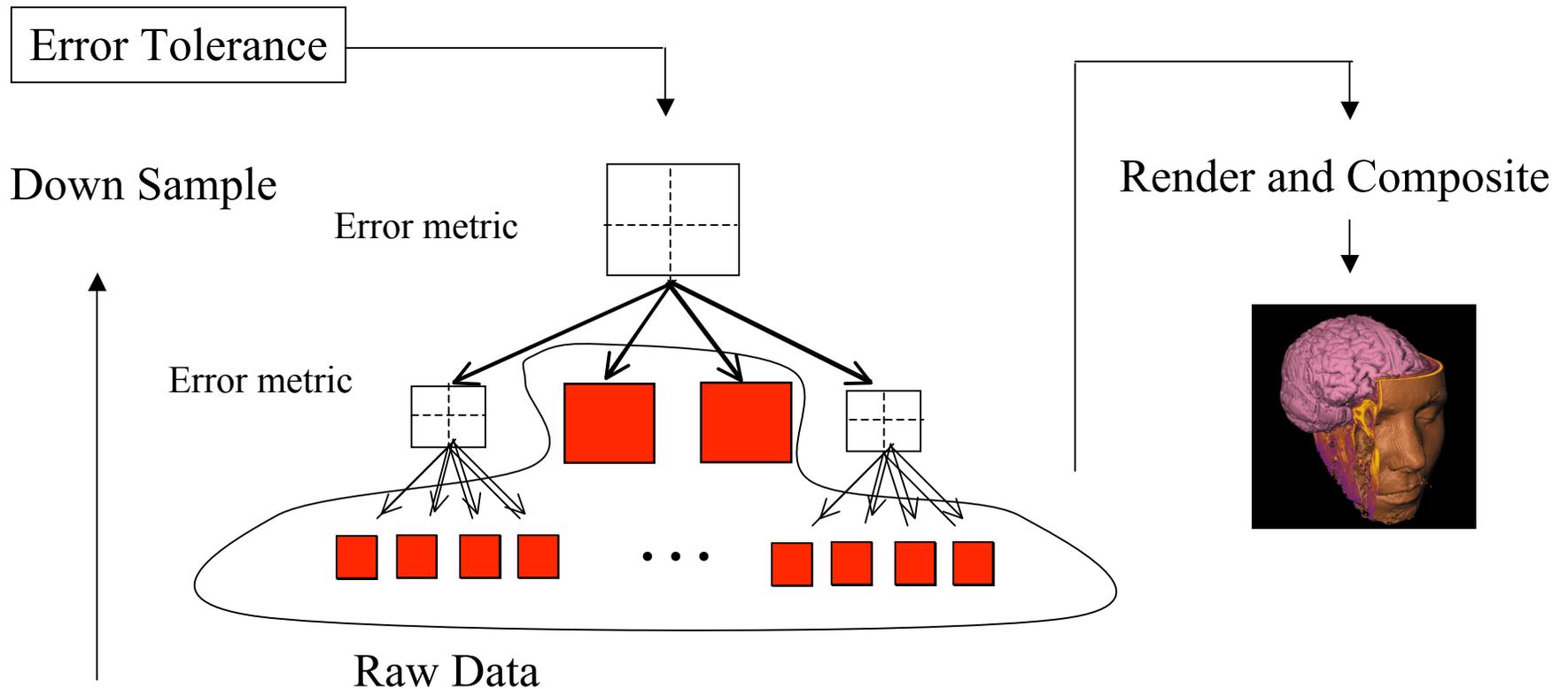
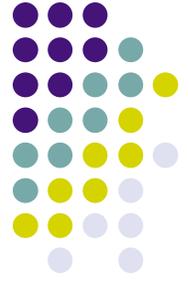


# Ultra Scale Data Exploration



- Large-scale data sets are common in both medical and scientific applications
- Large data size makes interactive visualization difficult
  - High memory/texture memory requirement
  - Slower rendering speed

# Multi-resolution Volume Rendering

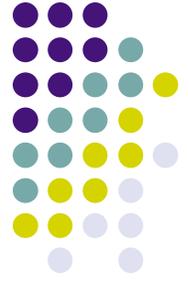


# Research Questions



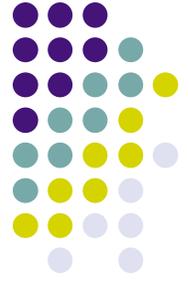
- How do we measure and compare the quality of different LOD selections?
- Are the computation resources effectively distributed?
- Can we visualize what are being visualized and make changes?

# Global LOD Quality Metric



- Measure the amount of information contained in the selected LOD
  - Compare LODs
  - Decide whether the computation resources are distributed evenly to render-worthy blocks
  - LOD adjustment
- Approach: Employ information theory

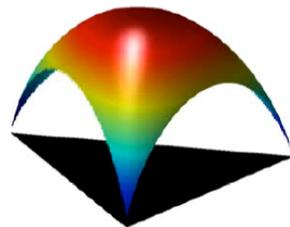
# Shannon Entropy



- The source of information takes a sequence of symbol  $\{a_1, a_2, a_3, \dots, a_M\}$  with probabilities  $\{p_1, p_2, p_3, \dots, p_M\}$
- The amount of information contained is defined as:

$$H(X) = - \sum_{i=1}^M p_i \log p_i$$

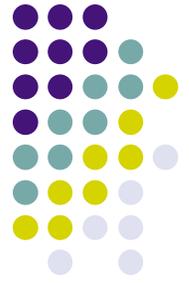
- Maximize the entropy function when  $P_i$  are all equal



An example of three dimensional Probability vector  $\{p_1, p_2, p_3\}$

# LOD Entropy

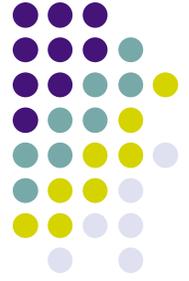
$$H(X) = - \sum_{i=1}^M p_i \log p_i$$



- A LOD contains a sequence of blocks  $B_i$  at particular resolutions
- $P_i$ , the ‘probability’ of a data block  $B_i$  at a particular resolution, is defined as:

$$p_i = \frac{\mathcal{C}_i \cdot \mathcal{D}_i}{S} \quad S = \sum_{i=1}^M \mathcal{C}_i \cdot \mathcal{D}_i$$

- $\mathcal{C}_i$  and  $\mathcal{D}_i$  are the block’s contribution and distortion (if it is a low resolution block)



# LOD Entropy

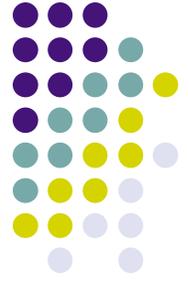
$$H(X) = - \sum_{i=1}^M p_i \log p_i$$

- The value of the entropy function is maximized when  $P_i$  are all equal

$$p_i = \frac{C_i \cdot D_i}{S}$$

$C_i \nearrow \Rightarrow D_i \searrow$  (high resolution)  
 $C_i \searrow \Rightarrow D_i \nearrow$  (low resolution)

The entropy function prefers that a block's resolution matches its contribution to the final image



# Contribution and Distortion

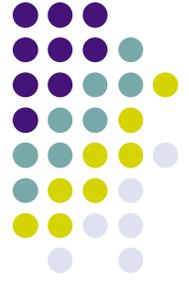
- Contribution: the block's color ( $\mu$ ), projection size ( $a$ ), thickness ( $t$ ), visibility ( $v$ )

$$\mathcal{C}_i = \mu \cdot t \cdot a \cdot v$$

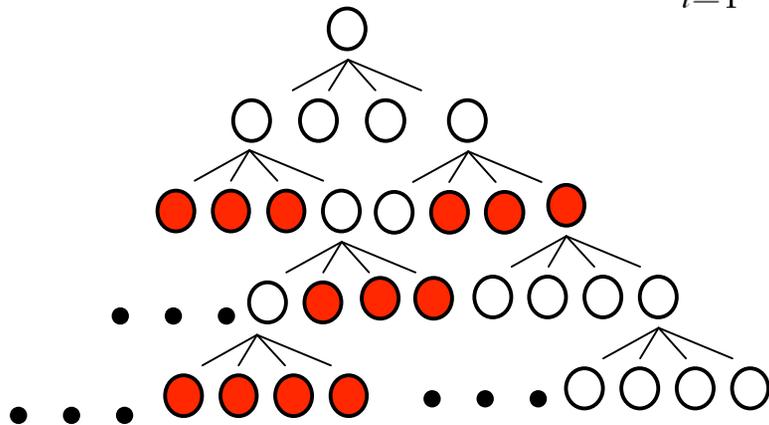
- Distortion: the difference between the block's data values and those of a higher resolution block

$$d_{ij} = \underbrace{\sigma_{ij}}_{\text{covariance}} \cdot \underbrace{\frac{\mu_i^2 + \mu_j^2 + C_1}{2\mu_i\mu_j + C_1}}_{\text{luminance}} \cdot \underbrace{\frac{\sigma_i^2 + \sigma_j^2 + C_2}{2\sigma_i\sigma_j + C_2}}_{\text{contrast}}$$

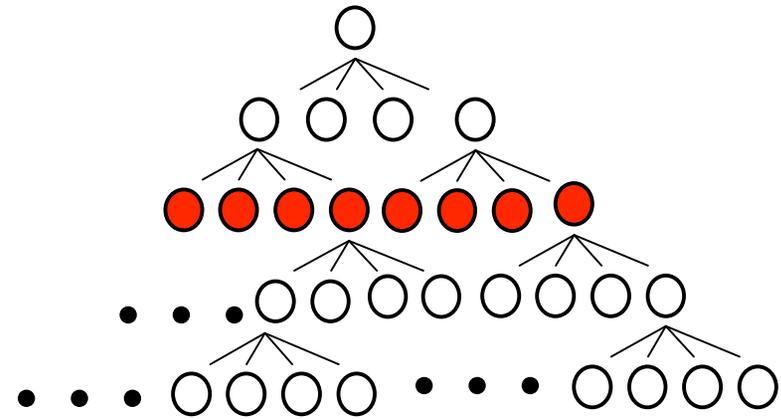
# LOD Comparisons using Entropy



$$H(X) = - \sum_{i=1}^M p_i \log p_i$$



H1



H2

A higher entropy value indicates a balanced probability distribution, thus a better overall quality

# Entropy vs. Quality



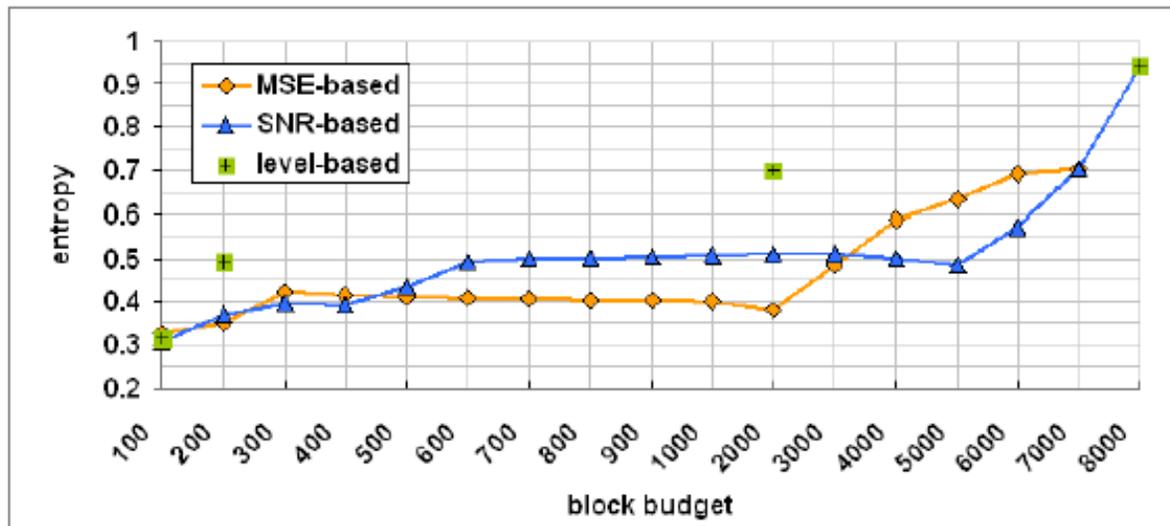
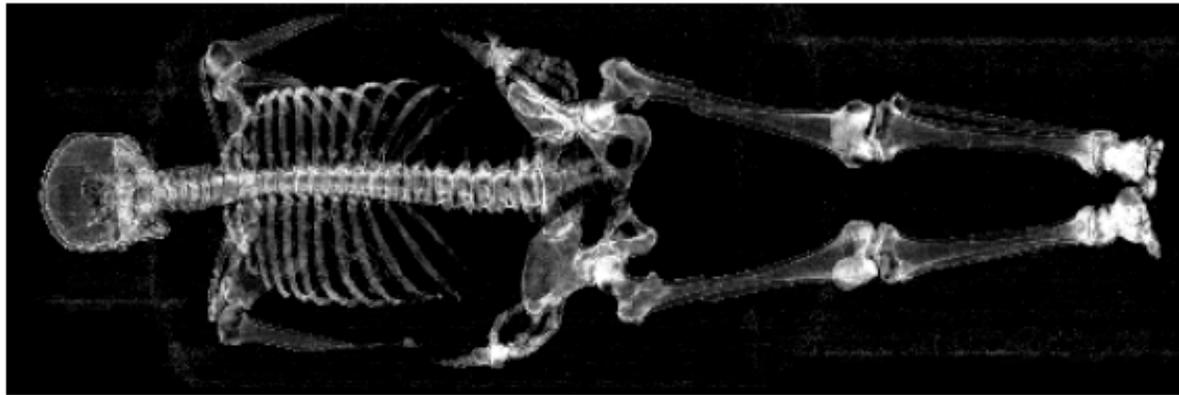
Entropy = 0.166 (34 blocks)



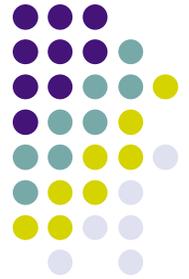
Entropy = 0.316 (259 blocks)



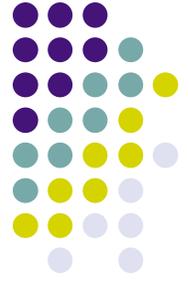
# Entropy vs. # of Blocks



# Visual Representation of LOD Quality

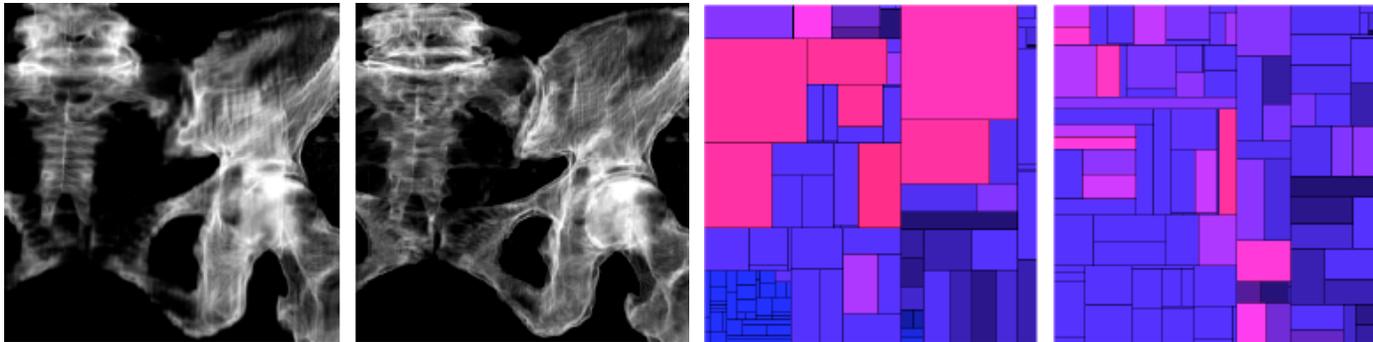


- An optimal selection of LOD is an NP complete problem
- Fine tuning of LOD selection is often necessary
- Can we visualize what are being selected, and make adjustments if necessary?

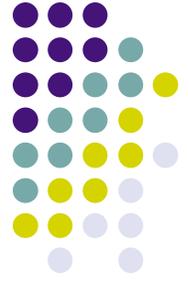


# LOD Map

- A visual user interface to visualize the LOD selection
- Allow the user to see individual block's contribution vs. distortion, i.e., visualize the entropy terms



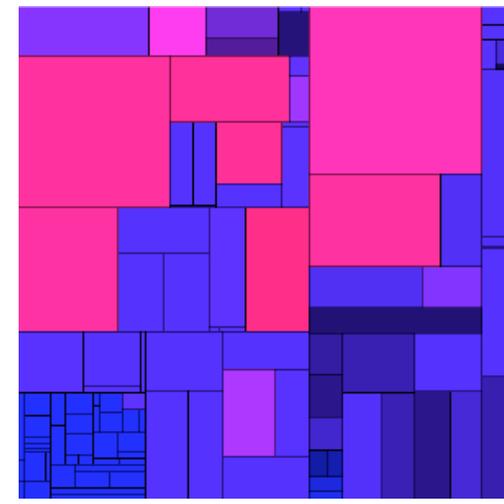
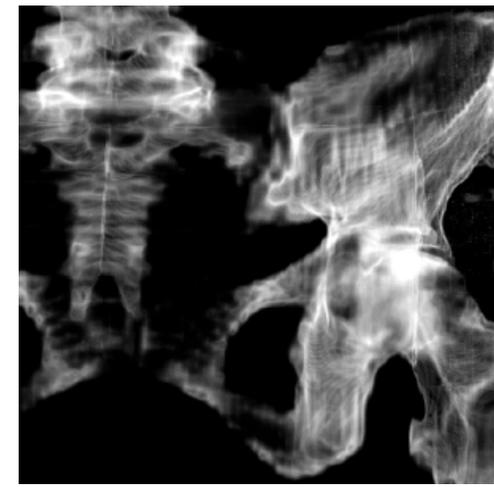
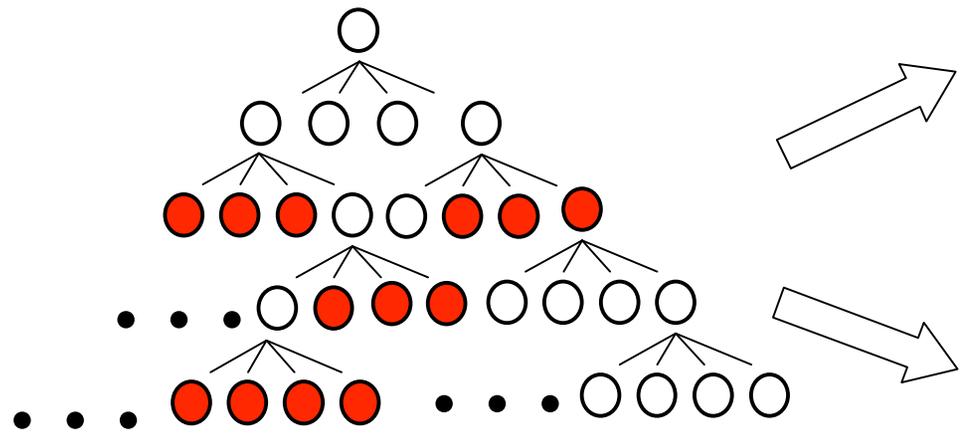




# LOD Map

- Display the blocks belong to the selected LOD in a tree-map like manner
- Color (blue to red) is used to encode the block's distortion ( $\mathcal{D}_i$ )
- The contribution of the block ( $\mu.t.a.v$ ) is divided into two parts
  - The size of rectangle is to encode  $\mu.t.a$
  - The opacity of rectangle is to encode  $v$

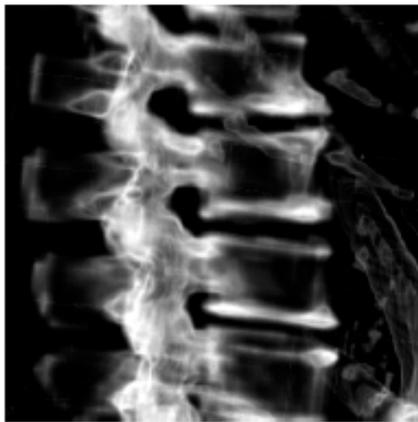
# LOD Map



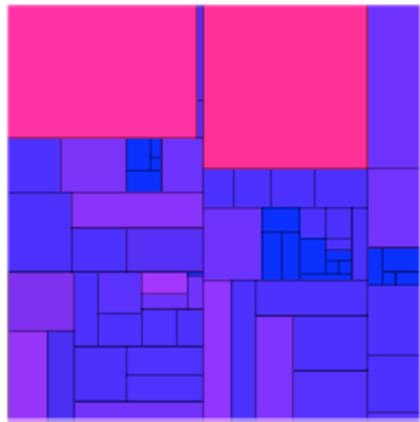
# How Can LOD Map Help



Comparisons of different LOD selection schemes



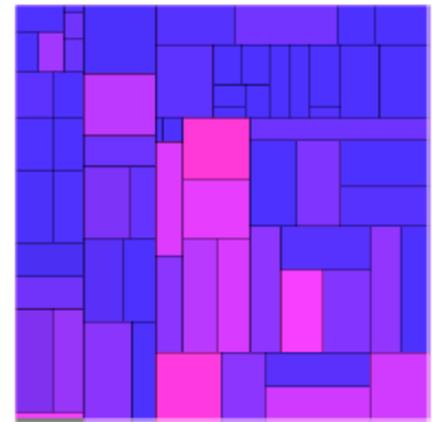
(a) MSE-based, 67 blocks



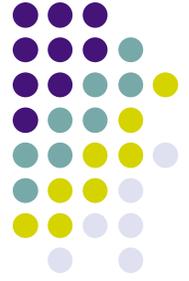
(b) entropy = 0.163



(c) level-based, 67 blocks



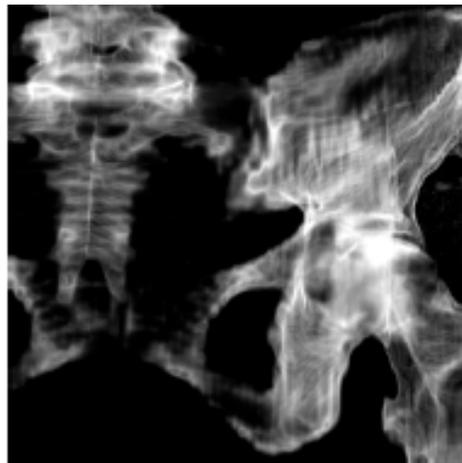
(d) entropy = 0.381



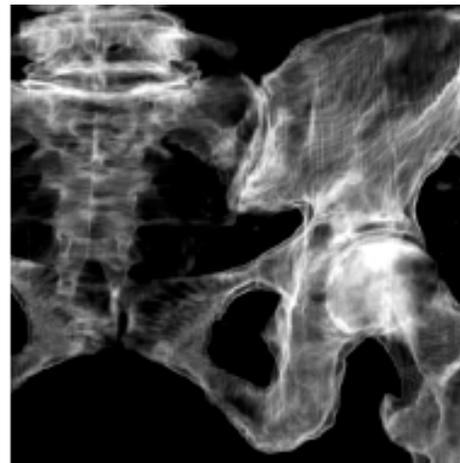
# How Can LOD Map Help

- Spot problematic regions in the current LOD
  - Large red rectangles – high contribution blocks rendered with low resolutions
    - Action: split the blocks and increase the resolutions
  - Small blue rectangles – low contribution blocks rendered with high resolutions
    - Action: join the blocks and reduce the resolutions
  - Dark rectangles – low visibility blocks
    - Action: join them and reduce the resolutions

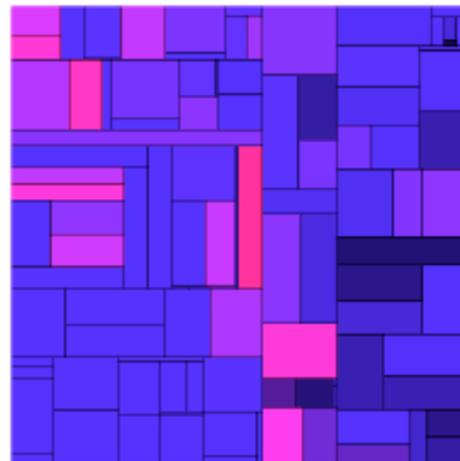
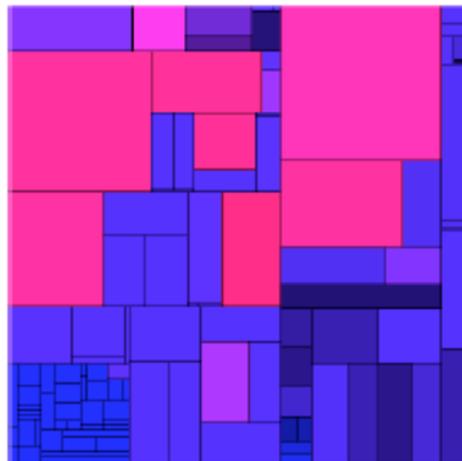
# LOD Adjustment

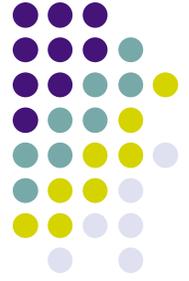


before, 108 blocks



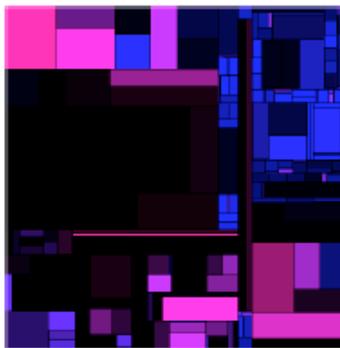
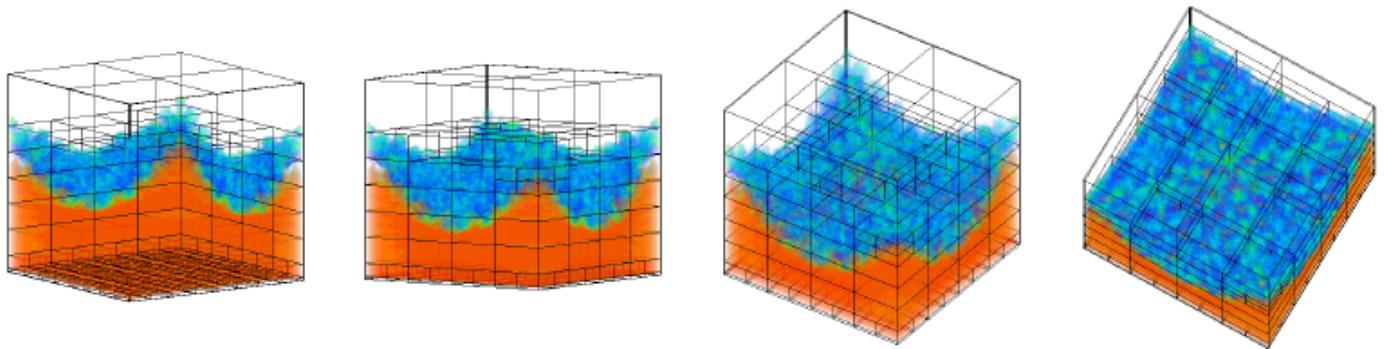
after, 108 blocks



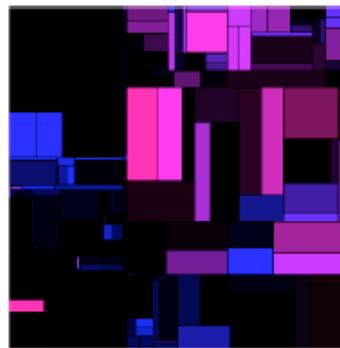


# How Can LOD Map Help

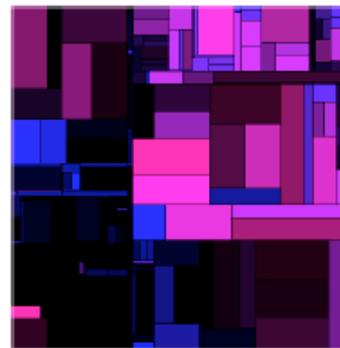
- View selection on the fly - High entropy and brighter LOD map for better views



(a) entropy = 0.330



(b) entropy = 0.343



(c) entropy = 0.384

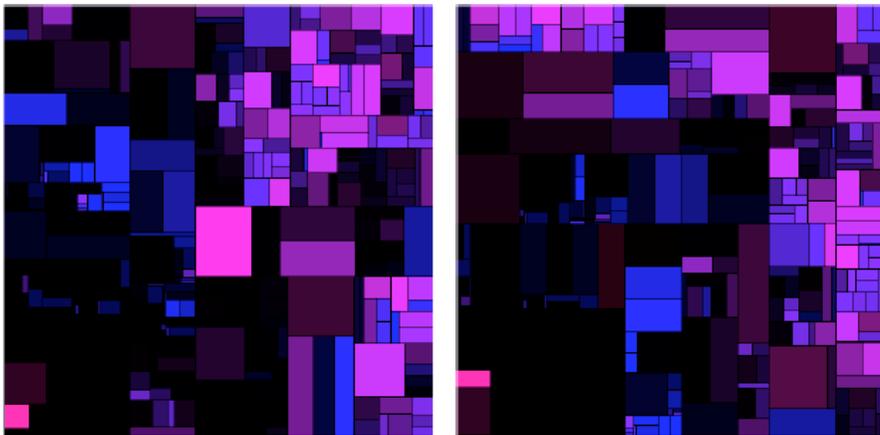


(d) entropy = 0.390

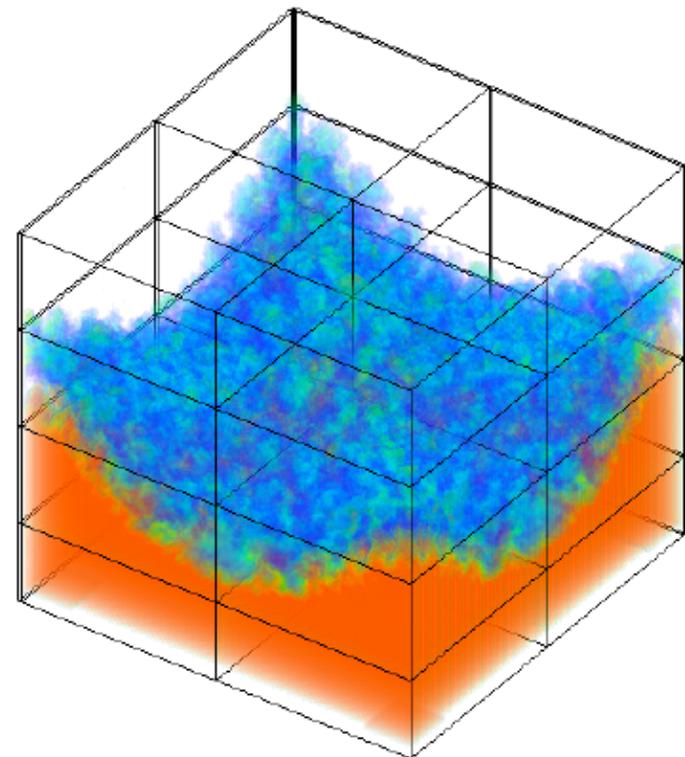


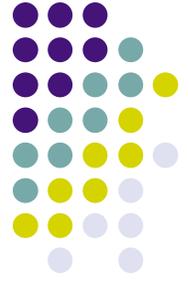
# How Can LOD Map Help

- Budget Control - Render fewer blocks, i.e., lower Resolutions in certain regions, for the same entropy



(a) entropy = 0.448, 365 blocks    (b) entropy = 0.476, 274 blocks

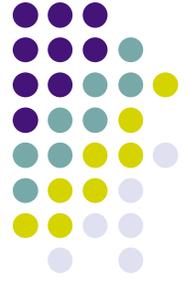




# Summary

- Entropy is used as a way to quantify the LOD quality
- LOD Map is used to provide visual feedback for the LOD adjustment
- An image based metric is used to measure the actual contribution of a block to the final image

# Acknowledgements



- NSF Career Award CCF-0346883
- DOE Early Career Principal Investigator Award DE-FG02-03ER25572
- NSF ITR grant ACI-0325934



National Science Foundation  
WHERE DISCOVERIES BEGIN