

# A Geoscience Perspective on Immersive 3D Gridded Data Visualization

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## Abstract

We describe visualization software, **Visualizer**, that was developed specifically for interactive, visual exploration in immersive virtual reality (VR) environments. Visualizer uses carefully optimized algorithms and data structures to support the high frame rates required for immersion and the real-time feedback required for interactivity. As an application developed for VR from the ground up, Visualizer realizes benefits that usually can not be achieved by software initially developed for the desktop and later ported to VR. However, Visualizer can also be used on desktop systems (unix/linux based operating systems including Mac OS X) with a similar level of real-time interactivity, bridging the “software gap” between desktop and VR that has been an obstacle for the adoption of VR methods in the Geosciences. While many of the capabilities of Visualizer are already available in other software packages used in a desktop environment, the features that distinguish Visualizer are: 1) Visualizer can be used in any VR environment including the desktop, GeoWall, or CAVE, 2) In non-desktop environments the user interacts with the data set directly using a wand or other input devices instead of working indirectly via dialog boxes or text input, 3) On the desktop, Visualizer provides real-time interaction with very large data sets that can not easily be viewed or manipulated in other software packages. Three case studies are presented that illustrate the direct scientific benefits realized by analyzing data or simulation results with Visualizer in a VR environment. We also address some of the main obstacles to widespread use of VR environments in scientific research with a user study that shows Visualizer is easy to learn and to use in a VR environment and can be as effective on desktop systems as native desktop applications.

*Key words:* 3D data visualization, virtual reality, immersive visualization, interactive exploration

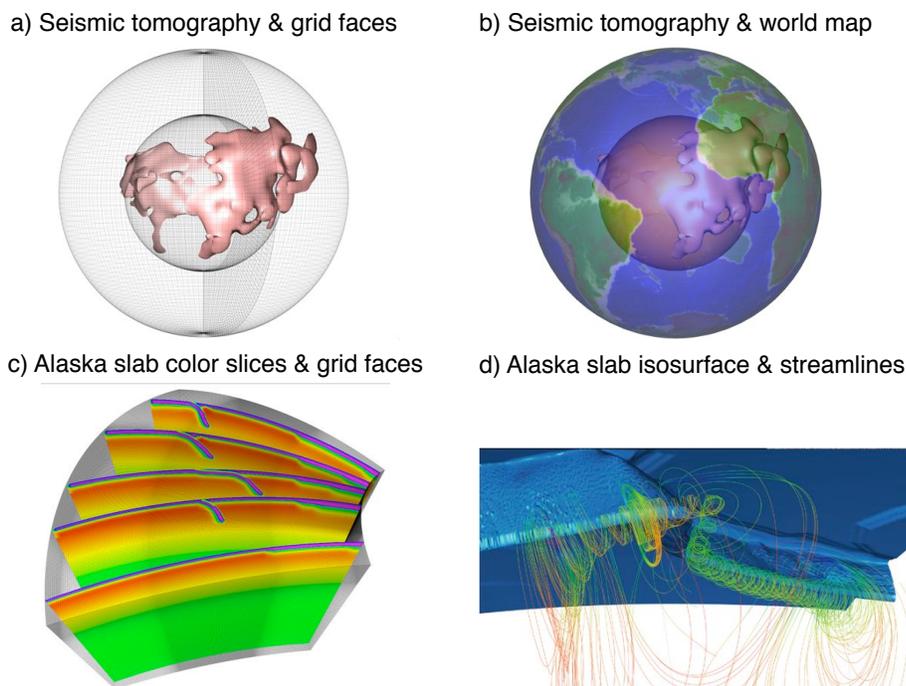


Fig. 1. Examples of geoscience gridded data sets illustrating the types of data that can be viewed with Visualizer. a) Seismic tomography model of mantle shear wave velocity with the spherical grid faces shown (Mégnin and Romanowicz, 2000). b) Seismic tomography model with world map superimposed for geographic reference. c) Color slices of the input viscosity structure for a subduction model of the Alaskan slab. d) Isosurface and streamlines for a numerical simulation of mantle flow near the Alaskan slab. See Movies 1–3 for demonstration of the Visualizer software.

## 1 Introduction

Geoscientists work with diverse data sets ranging in spatial scales from nanometers to thousands of kilometers and varying on time scales from femtoseconds to billions of years. Typically, these observations, or the results of numerical simulations, are 3D gridded data sets: seismic tomography images of the Earth’s interior, finite element models of mantle convection, atmospheric mixing and oceanic currents, or fossils imaged in ancient rocks. Analyzing and interpreting these large volumetric data sets with information at multiple scales poses a significant challenge in geoscience research – one that can be addressed by the scientific visualization community, particularly through innovative use of interactive and immersive virtual reality (VR) environments (Lin and Loftin, 1998; Rhyne and MacEachren, 2004; Kreylos et al., 2006b). For example, analysis of complex geodynamic simulation results from one

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11 of the world’s largest supercomputers, the Earth Simulator in Japan, has been found to benefit from  
12 visualization and direct manipulation in a CAVE VR system (Furumura and Chen, 2004; Ohno and  
13 Kageyama, 2007).

14 A substantial component of research in the geosciences involves identifying the most important pro-  
15 cesses in natural systems and developing computational models of key interactions. One efficient way  
16 to identify unknown processes is to look for correlations within and among data sets. Quantitative  
17 evaluation of correlations requires the scientist to have a detailed conceptual model of the underlying  
18 relationships; however, the fundamental processes are poorly constrained for many of the problems at  
19 the forefront of research. Thus, correlations can be extremely difficult to predict and extract mathe-  
20 matically. In addition, while statistical and graphical information derived from computer simulations  
21 or observational data are important characterizations, by their very nature, they limit the amount  
22 and type of information conveyed. In these cases, relationships among data are best identified by ex-  
23 amining data visually in a flexible, interactive environment that takes full advantage of the human  
24 brain’s ability to visually identify patterns, outliers and unexpected or abnormal features. Such visual  
25 examination of data can lead to the conceptual framework necessary to develop quantitative methods  
26 for further analysis.

27 Different software packages provide different methods with which to display and manipulate 3D gridded  
28 data sets, from clicking and dragging with a mouse to entering values via a keyboard. Throughout this  
29 article we use the term ”interactive” to describe software that allows the user to directly manipulate  
30 visualization objects in real-time in a manner similar to how one would interact with a real object.  
31 To give two examples, 1) as opposed to the IVS 3D Fledermaus software (Fledermaus, 2007), where  
32 users change views by manipulating special rotation widgets with the mouse, Visualizer allows users  
33 to directly grab and rotate an object with the mouse or other input device, and 2) instead of entering  
34 the value for a desired isosurface numerically, Visualizer allows users to create isosurfaces passing  
35 through any point in the data’s domain by selecting a point with the mouse or other input device, and  
36 to drag newly created isosurfaces in real time. This type of direct interactive visualization provides  
37 many advantages over other visualization approaches, not the least because it is intuitive and more  
38 natural than other approaches. However, it also places high demands on the software to respond  
39 in real time and to reproduce a real-world-like virtual space for data analysis. For example, in an  
40 immersive environment such as a CAVE, a user can create an isosurface by touching a point in the  
41 data’s domain using a tracked input device such as a wand, leading to very natural interactions. On a  
42 desktop system, on the other hand, the software has to provide more involved interaction mechanisms  
43 to support intuitive and unambiguous 3D point selection using only the mouse, a 2D input device.

44 In 2003 a collaboration between computational scientists and geoscientists at U.C. Davis directed at  
45 developing scientific visualization methods and effective systems was formed in conjunction with the W.  
46 M. Keck Center for Active Visualization in the Earth Sciences, *KeckCAVES* (<http://www.keckcaves.org>).  
47 This collaborative effort is currently concerned with a range of scientific visualization problems includ-  
48 ing data quality and scientific analysis of LiDAR (Light Detection And Ranging) data sets of 10–350  
49 GB in size (Kreylos et al., 2006a; Bawden, 2006), mapping on digital terrain data sets (Remote Interac-  
50 tive Mapping System (RIMS), Bernardin et al. (2006)), and model assessment and scientific analysis of  
51 3D gridded data (Jadamec and Billen, 2006) (Figure 1). We discuss one of the software systems emerg-  
52 ing from this collaboration, *Visualizer*, developed for analyzing 3D gridded data sets in an interactive,

53 immersive VR environment. Although the underlying VR Toolkit that Visualizer is built on (Vrui,  
54 (Kreylos et al., 2006a)) is capable of interfacing with real-time simulations to visualize dynamically  
55 evolving objects (Tipper, 1991), Visualizer has been developed to optimize the interactive experience  
56 with a single, unchanging, object. This software and instructions for installation and use are available  
57 for free download from the KeckCAVES website (<http://www.keckcaves.org/software/index.html>).

58 Visualization of 3D gridded data is not new, and is certainly not new to the Geosciences. For exam-  
59 ple, the results of 3D structures in seismic tomographic images and mantle convection models have  
60 commonly been presented as combinations of isosurfaces and color-mapped slices (Méglin and Ro-  
61 manowicz, 2000; Tackley, 2000; Furumura and Chen, 2004; McNamara and Zhong, 2005; Wang et al.,  
62 2007), 3D seismic reflection-refraction data is presented as 3D rendered volumes or movies of color  
63 slices (Lin and Loftin, 1998; Gao, 2003; Ma and Rokne, 2004), and 3D reconstructions of fossils has  
64 been used to study biomechanics of extinct species (Kalvin et al., 1992; Sutton et al., 2001; Zollikofer  
65 and de Leon, 2005; Motani et al., 2005). However, visualization software has historically been divided  
66 between desktop and VR environments, forcing users to learn to use two or more applications in order  
67 to move between the realms. Additionally, the design of the software was focused more on producing  
68 a final image than facilitating exploration of the data set. In the following sections we discuss the  
69 motivation for developing a new software package for visualizing 3D gridded data in the Geosciences  
70 (sections 1.1–1.2), how this software is similar to or different from other existing software packages  
71 (section 2.0), how the software achieves real-time interactivity (sections 3.0–4.0), and three case studies  
72 and a user study illustrating how the software facilitates efficient and effective data exploration and  
73 analysis (section 5.0). Visualizer is a complex software package built upon a complex development  
74 toolkit for virtual reality applications (Kreylos, 2006). Therefore, we limit our discussion of its design  
75 and implementation to those aspects that users will most directly interact with, and that are essential  
76 for providing an intuitive environment for data exploration. As it is sometimes difficult to fully com-  
77 municate the experience of using this software in a CAVE environment using words and still images,  
78 we strongly encourage the reader to view the accompanying movies showing the software being used  
79 in a CAVE (Movies 1 and 3) and on the desktop (Movie 2).

### 80 *1.1 Why Use a 3D Immersive Environment?*

81 Research on human visual perception of the world attests to the complexity and power of human visual  
82 ability. We perceive a 3D world primarily through a combination of binocular vision and the use of  
83 motion parallax (Harris, 2004). However, the brain obtains many clues as to the depth and shape of  
84 objects from the surrounding environment (ground-plane, shadows, relative motion). Immersive envi-  
85 ronments allow scientists to take advantage of the way the brain already interprets visual information  
86 (Hubona and Shirah, 2005) and provides key advantages for evaluating and analyzing Earth science  
87 data and simulations, including use of peripheral vision to provide global context, body-centric judge-  
88 ments about 3D spatial relations and enhanced 3D perception from stereo and motion parallax (head  
89 tracking) (van Dam et al., 2000). Together these spatial indicators create a more natural environment  
90 and thus promote more efficient exploration of 3D data. On a regular computer screen, the strongest  
91 available depth cue is motion parallax. As a result, to understand 3D data from images on a screen,  
92 users need to constantly rotate the view or rock it back and forth to perceive depth. This motion

93 interferes with detailed examination or measurement of the displayed data, and is not required in  
94 stereoscopic environments where other depth cues are available. Furthermore, immersive environments  
95 – offering head tracking in addition to stereoscopy – enable motion parallax without the user having  
96 to consciously move the 3D data: motion is simply created by moving one’s head or walking around  
97 the data; an intuitive response that does not interfere with analysis tasks.

98 While the use of proprietary software in 3D immersive environments in industrial applications has  
99 spread in recent years, and despite the possible advantages for scientific discovery, the use of immersive  
100 technology in scientific research has not grown as quickly (van Dam et al., 2000). Several concerns  
101 arise in evaluating the role of 3D immersive VR for scientific applications. Is anything new learned  
102 from viewing data in a 3D immersive VR environment? How do we quantify what is seen? Does  
103 the 3D viewing provide a real advantage over viewing multiple 2D slices or 2D images on a computer  
104 screen? Does using a 3D immersive environment save time? Are 3D immersive environments sufficiently  
105 accessible/available? The answers to each of these questions vary depending on the data type, size of  
106 data, and type of 3D environment considered. For example, only a few academic research groups (less  
107 than 10) in the U. S. have regular access to a CAVE environment, but more than 500 have access  
108 to a GeoWall (Johnson et al., 2006). With the continued decrease in cost of stereo-capable projection  
109 systems based on polarization (“passive stereo”), frame interlacing (“active stereo”), or other methods,  
110 GeoWall-type 3D immersive environments could become commonplace. However, this will only happen  
111 if software is already available that is easy to use and provides all the capabilities scientists require.

112 As we look to the future of larger and more complex data sets and model results, we would like to  
113 prepare for the time when the current ways of carrying out scientific analyses are no longer effective  
114 or time-efficient. Is it possible to create software for 3D immersive VR environments that is easy-  
115 to-use and provides an effective and efficient tool for scientific analysis? The range in types of data  
116 and applications found in the Earth Sciences provides an ideal testing ground for developing such  
117 software. We present one software system designed with this long-term perspective in mind. This  
118 software does not provide everything one would need or want, but it demonstrates one way of bridging  
119 the visualization methods we are accustomed to on the desktop to a new way of analyzing data in 3D  
120 immersive VR environments.

## 121 *1.2 Visualizer: 3D Volume Visualization Software.*

122 It has long been known that graphical representations of complicated data sets on 2D displays provide  
123 efficient and insightful ways of interpreting quantitative data (Tufte, 1983), but similar analysis of 3D  
124 data sets using 3D visualization has lagged behind. One reason may be that the design of 3D volume  
125 visualization software has traditionally focused on providing an environment for users to create a  
126 final image of a data set that is effective at communicating ideas and results (TecPlot, 2006; Vis5D,  
127 2006; CAVE5D, 2006). This type of visualization software usually facilitates enhancing the appearance  
128 of structures of interest, or synthesizing various data types, e. g., isosurface of temperature, color-  
129 mapped slices of viscosity or stream-tubes of fluid flow in a numerical fluid dynamics model. However,  
130 this design objective is focused on visualizing known structures, such as when the value of the best  
131 isosurface to display is already known. However, this approach does not support exploring a data

132 set in which the features of interest are yet to be discovered. Exploring a data set visually in order  
133 to identify features or processes of scientific interest requires an interactive environment and real-  
134 time visualizations that can be modified on-the-fly. In addition to making the software adaptable to  
135 different geoscience applications, it must be straight-forward to load data sets of various formats into  
136 the software, and easy to learn and use.

137 The 3D volume visualization software presented here, called Visualizer, has been specifically designed  
138 for highly interactive 3D VR environments and therefore follows different design principles than soft-  
139 ware that was originally developed for use in a 2D desktop environment (Bowman et al., 2004). For  
140 example: 1) navigating (picking up, rotating and translating a slice or isosurface) in a VR environment  
141 is simply done by moving a tracked input device, such as a wand, while pushing a button, 2) intuitive  
142 direct manipulation, such as creating isosurfaces by touching a seed point using a tracked input device,  
143 is favored over indirect methods such as entering numbers, and 3) creating isosurfaces or slices occurs  
144 in real time as an input device is moved through a virtual data set.

## 145 2 Related Work

146 To put Visualizer into context, and compare it to other 3D visualization software for desktop and  
147 immersive environments, we first discuss several desktop applications, and then several applications  
148 developed for VR (Table 1).

149 **TecPlot** (TecPlot, 2006) is a commercial visualization software for 3D volume data in a desktop  
150 environment, and is widely used in the Earth sciences. Its main goal is the production of publication-  
151 quality graphs and figures, but it also contains several features that make it applicable to visual  
152 data analysis. Its main volume *visualization elements* are color-mapped slices and isosurfaces, and  
153 the program allows one to change the set of elements interactively. However, interaction is limited to  
154 entering desired isovalues into dialog boxes or dragging axis-aligned slices through a data set using  
155 sliders in a dialog box. The program’s response to changes is not in real time: especially changing  
156 an isovalue causes delays of tens of seconds before the display is updated. We found that directly  
157 observing the changing shape of an isosurface under varying isovalues is a very powerful analysis tool  
158 (see Movie 3); the fact that TecPlot does not support this style of exploration is a major limitation.  
159 Additionally, TecPlot’s navigation methods are limited when a user wants to explore a small feature in  
160 a larger data set in detail. Although TecPlot provides the usual virtual trackball interface, it can only  
161 rotate the data around its centroid, not around arbitrary 3D points. This, and the fact that TecPlot  
162 reduces the resolution of surfaces during navigation, severely limit detail analysis. TecPlot does contain  
163 a measurement tool to query the spatial position of and data values at arbitrary locations, but it is  
164 not intuitively clear how TecPlot translates a 2D mouse position into 3D space for measurement.

165 **Vis5D** (Vis5D, 2006) is an open-source visualization software aimed at time-varying, multivariate 3D  
166 volume data. It is often used in the Earth sciences, especially in atmospheric science. Its main goal  
167 is the production of figures and animations. Vis5D’s main visualization elements are color-mapped  
168 slices and isosurfaces, but it also supports direct volume rendering. The level of interactivity of Vis5D  
169 is similar to TecPlot’s, with the same limitations for visual data analysis, but Vis5D contains some

EXAMPLES OF COMMONLY-USED SOFTWARE

Software	Positive Features	Negative Features
<u>Desktop Applications</u>		
TecPlot	<ul style="list-style-type: none"> <li>- easy to learn</li> <li>- easy to input data</li> <li>- multiple input data types</li> <li>- measurement tools</li> <li>- virtual trackball rotation (VTR)</li> </ul>	<ul style="list-style-type: none"> <li>- enter slice location/desired isovalues into dialog box</li> <li>- response to use changes is not real-time (&gt;10-60 s)</li> <li>- image resolution reduced during rotation/translation</li> <li>- difficult to determine location of measurement in 3D</li> <li>- VTR limited to rotation around data centroid</li> </ul>
Vis5D	<ul style="list-style-type: none"> <li>- easy to learn</li> <li>- measurement tools</li> <li>- direct volume rendering</li> <li>- slices can be dragged through data</li> <li>- VTR around screen-center</li> <li>- animations</li> </ul>	<ul style="list-style-type: none"> <li>- enter slice location/desired isovalues in dialog box</li> <li>- difficult to determine location of measurement in 3D</li> <li>- long rendering times for isosurfaces</li> </ul>
<u>VR Environment Applications</u>		
CAVE5D	<ul style="list-style-type: none"> <li>- direct port of Vis5D</li> <li>- slices can be dragged through data</li> </ul>	<ul style="list-style-type: none"> <li>- slices must be dragged by box corner</li> <li>- change isosurface value in virtual dialog box</li> <li>- model rotates around its centroid or user's head</li> <li>- non-intuitive navigation is difficult to learn</li> </ul>
NASA's Virtual Wind Tunnel	<ul style="list-style-type: none"> <li>- developed for VR environment</li> <li>- direct 3D manipulation of data</li> <li>- real-time rendering</li> <li>- seeded slices and isosurfaces</li> <li>- grab space navigation</li> <li>- grab space data manipulation</li> </ul>	<ul style="list-style-type: none"> <li>- only portable to limited range of VR environments</li> <li>- only one grid format for input</li> </ul>

Table 1

Examples of visualization software commonly-used in the geoscience community summarizing some of the positive and negative features of the software evaluated for interactive 3D visualization.

170 improvements: slices can be dragged by direct manipulation with the mouse, and the virtual trackball  
 171 for navigation always rotates around the screen center, improving the user's ability to examine small  
 172 features in detail. Vis5D's volume rendering feature uses a simple slice-based algorithm, and is due to  
 173 its long rendering times is not applicable to interactive exploration.

174 **CAVE5D** (CAVE5D, 2006) is a direct port of Vis5D to immersive environments based on the CAVE  
 175 (Computer Assisted Virtual Environment) library (Cruz-Neira et al., 1993). It runs in VR environments  
 176 compatible with CAVELib, and uses a CAVE wand to control the visualization. Even though CAVE5D  
 177 was introduced in late 1995, it is still used for Earth science visualization in immersive environments,  
 178 especially CAVEs. One reason might be that it allows scientists to visualize data on the desktop  
 179 first using Vis5D, and then to import the visualizations into a CAVE (e.g., a four-walled immersive

180 visualization environment).

181 The development of CAVE5D from Vis5D is a good example of the challenges posed by porting  
182 desktop software to immersive environments. The main benefits of VR, intuitive navigation and direct  
183 manipulation of 3D objects, are not realized because the original desktop program does not contain  
184 functionality to support them. For example, Vis5D allows a user to drag a slice by manipulating it with  
185 the mouse, and CAVE5D uses the same mechanism, but based on a 6-DOF input device. Instead of  
186 just moving the device to a position of interest and pressing a button to create a slice at that position  
187 (or drag an existing slice), the user has to aim the device at an “interaction box” at the corner of the  
188 slice to drag the slice along its axis. This makes it quite difficult to change a slice while zoomed-in to  
189 examine a feature, and is not the most appropriate way of using a 6-DOF input device to manipulate  
190 a 3D object. Interestingly, isosurfaces are still changed by numerically entering a desired isovalue;  
191 however, since VR environments have no keyboards, users have to use the wand to enter numbers via  
192 a virtual 3D keypad. This style of interaction is actually less effective in a VR environment than on  
193 a desktop. Navigation also does not take full advantage of interaction using a 6-DOF input device:  
194 rotating the wand causes the data set to rotate, but not around the current position of the wand.  
195 Instead, the model rotates either around its centroid or the user’s head position, depending on the  
196 navigation mode. Both navigation modes are hard to learn, and even experienced users sometimes have  
197 problems moving a model in the desired way. As a result, CAVE5D is mostly used to present previously  
198 created visualizations in a more impressive environment, and not to create or analyze visualizations  
199 by interactive exploration.

200 **The NASA virtual wind tunnel** (Bryson and Levit, 1991; Meyer and Globus, 1993; Bryson, 1996)  
201 is an even older application than CAVE5D, but it was directly developed for immersive environments  
202 and takes into account the particular benefits and constraints of VR. Its main purpose, as the name  
203 implies, is the analysis of computational fluid dynamics data, but it could be used for other 3D volume  
204 data as well. Its main visualization elements are streamlines/streaklines, particle traces, color-mapped  
205 slices, and isosurfaces. As opposed to CAVE5D, all visualization algorithms are optimized for direct  
206 3D manipulation and real-time feedback. For example, streamlines are created by directly selecting  
207 their starting point in 3D space, and isosurfaces are created by growing them from a selected seed  
208 point in space, instead of specifying their isovalue. Isosurfaces are based on time-outs, i. e., the result  
209 of creating a surface will be visible in the display in less than 0.1 s, enabling direct observation of an  
210 isosurface’s change as the seed point is dragged (see section 4.2 for description of seeded algorithms).  
211 Navigation is also intuitive: users can “grab space” using a 6-DOF input device, and then reposition  
212 the data set by moving/rotating the input device. Overall, the virtual wind tunnel is an effective visual  
213 analysis application. Its main limitations are that it only supports a single grid format and that it is  
214 only portable to a very limited range of VR environments.

### 215 **3 Interactive Exploration of 3D Volume Data**

216 In the development of the Visualizer software, we followed many of the design principles first exhibited  
217 by the NASA virtual wind tunnel (Bryson and Levit, 1991) and later described in more detail in (Sher-  
218 man and Craig, 2002). These design principles are summarized in Table 2 and described in more detail

KEY DESIGN FEATURES OF THE VISUALIZER SOFTWARE

Element	Description
Virtual Reality	High Frame rates (>30 Hz) for head-tracked stereo-viewing – Real-time response to user interaction (< 1/10 s)
Interaction	Display can not "freeze" during rendering – intermediate results presented in < 1/10 s – generated triangle set rendered in < 1/30 s Direct manipulation for navigation, element creation and manipulation – grab space ability – point-and-click selection of visualization elements
Portability	Use same software in multiple environments – built on VRUI development tool-kit – Visualizer is completely independent of underlying VR environment – Optimal matching of interaction patterns to capabilities of underlying environment
Multiple Grid Formats	Supports wide range of input data types – regular (Cartesian), hexahedral (curvilinear), simplicial (tetrahedral) grids, and heterogeneous FEM meshes – optimized visualization algorithms implemented for different data types

Table 2

Key design features in the Visualizer software required for interaction in VR environments and use in geoscience applications.

219 here. Three movies also illustrate how these design principles create an efficient and effective tool for  
220 exploration of 3D volume data on the desktop or in a CAVE (see online supplementary material).

221 The two main constraints of VR are the high frame rates upwards of 30 Hz required for head-tracked  
222 stereo viewing, and real-time response to any user interaction within 1/10 s (Bryson, 1996; Kreylos  
223 et al., 2001). These constraints influence the implementation of all visualization algorithms, whose  
224 "standard implementations" typically do not observe them. A standard Marching Cubes (Lorensen  
225 and Cline, 1987) implementation, for example, might require several seconds or minutes to generate  
226 millions of triangles for larger data sets. An interactive and immersive implementation of this algorithm  
227 must ensure that the display does not "freeze" during that time, that at least intermediate results are  
228 presented to the user after at most 1/10s, and that the generated triangle set can later be rendered at  
229 frame rates upwards of 30 Hz (Bryson and Levit, 1991). These goals require multithreaded program-  
230 ming (Lewis and Berg, 1998), special algorithms such as seeded isosurfaces (Meyer and Globus, 1993;  
231 Kreylos et al., 2001), advanced rendering using compressed geometry or multiresolution methods (En-  
232 gel et al., 1999), and careful optimization of the extraction and rendering algorithms.

233 The main benefits of VR are the direct 3D perception enabled by head-tracked stereoscopic displays and  
234 the ease with which users can select positions in 3D space using 6-DOF input devices. To fully exploit  
235 these benefits, visualization software has to follow a direct manipulation approach (Shneiderman,  
236 1983) across the entire range of functionality, from navigation over creation of visualization elements  
237 to quantitative analysis. If users see a feature of interest in a data set, they must be able to quickly

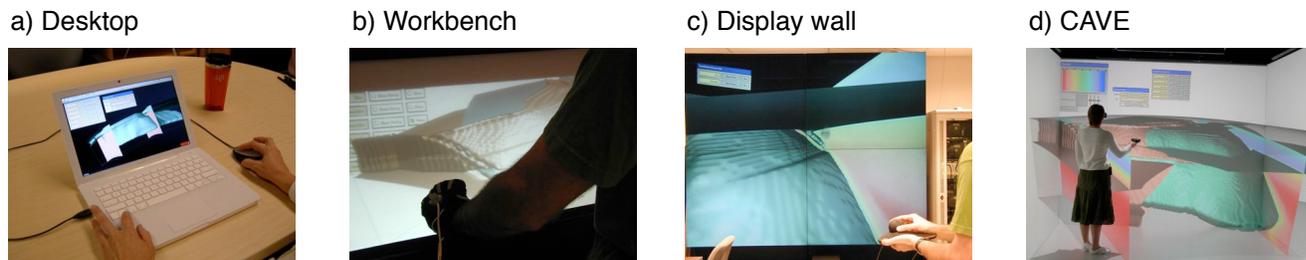


Fig. 2. The Visualizer application in four different VR environments: a) desktop, b) responsive workbench, c) tiled display wall, and b) CAVE. Visualizer achieves this cross-system portability by being built on the VRUI development toolkit (Kreylos, 2006), being completely independent of the underlying VR environment and optimally matching interaction patterns to the capabilities of the underlying environment.

238 create appropriate visualization elements to explore the feature in more detail; it is not appropriate to  
 239 first have to measure the position of or the data value at the feature, and then enter those numbers into  
 240 text fields to create slices or isosurfaces. Instead, VR software should allow users to create elements  
 241 by “point-and-click.” For example (Movie 3), when looking for connections between fossil structures  
 242 in rocks, dragging the wand through the data to create isosurfaces allows the user to determine if the  
 243 feature of interest is isolated or at what iso-value it is connected to nearby structures.

244 An additional important design goal is the ability to run the visualization application effectively on a  
 245 wide range of VR environments with different sets of input devices, including desktop environments  
 246 with only a mouse and keyboard (Figure 2). Our experience has shown that scientists are reluctant to  
 247 use VR software because it forces them to use a (shared) VR environment for all their analytical work,  
 248 or become proficient with two or more different visualization applications. Being able to use the same  
 249 VR software on the desktop or low-cost GeoWall-like environment first for preview generation and  
 250 initial quality assessment, and then only perform important and detailed explorations in VR alleviates  
 251 these concerns and should lead to a wider acceptance of VR methods in scientific domains. To achieve  
 252 maximum portability, we developed Visualizer on top of the Vrui VR development toolkit (Kreylos,  
 253 2006). Vrui supports highly interactive and high-performance VR applications that are completely  
 254 independent of the underlying VR environment, including the type and number of available input  
 255 devices. For example, Visualizer’s direct manipulation paradigm relies on a user’s ability to select  
 256 arbitrary points in 3D space. In an immersive environment, this is achieved by directly touching points  
 257 with a 6-DOF input device. On the desktop, on the other hand, users are limited to 2D interactions  
 258 using mouse and keyboard. Here, Visualizer (through Vrui) implements 3D point selection as an  
 259 extension of the virtual trackball-based navigation mechanism. Users can rotate the view around the  
 260 current screen center, can translate (pan) the view parallel to the screen plane, and can translate  
 261 (dolly) the view orthogonally to the screen plane. This means it is possible, and efficient after some  
 262 practice, to bring any arbitrary 3D point into the screen plane, and then select it by clicking it with  
 263 the mouse. As a result, Visualizer’s approach to data exploration works well even on desktop systems,  
 264 and our user study, discussed in Section 5, shows that while Visualizer is very effective in a CAVE, it  
 265 is also effective in a desktop environment – sometimes as effective, or even more so, than other native  
 266 desktop visualization applications.

267 Finally, we designed Visualizer such that it can be applied to a wide range of data formats. The differ-

268 ences between data formats such as regular (Cartesian), hexahedral (curvilinear), simplicial (tetrahe-  
269 dral) grids, and heterogeneous finite-element meshes are so fundamental that each normally requires  
270 its own implementation of all visualization algorithms (Shen and Johnson, 1995; Lorensen and Cline,  
271 1987). As VR software must be carefully optimized to satisfy VR’s real-time constraints, a software  
272 architecture should allow easy experimentation with different algorithms and data structures. For ex-  
273 ample, developers might have to change the representation of isosurfaces from individual triangles to  
274 indexed triangles or triangle strips to evaluate which performs best on a given system (Engel et al.,  
275 1999). If there are separate implementations of the underlying algorithms for different data formats,  
276 applying such changes while keeping all versions working together is a major software engineering  
277 challenge. As a result, most visualization programs, especially VR visualization programs, support  
278 only a single data format. Visualizer is based on a separation between data formats and algorithms  
279 that allows one to develop visualization algorithms only once, and apply them to all supported data  
280 formats. In fact, Visualizer only contains a single piece of code implementing its isosurface extraction  
281 algorithm, and this code is applied to regular, hexahedral, and tetrahedral grids (for more on isosurface  
282 extraction methods, see Shen and Johnson (1995); Lorensen and Cline (1987)). This data format and  
283 algorithm abstraction uses the C++ template mechanism (Alexandrescu, 2001; Stroustrup, 1997) to  
284 create highly efficient code that, according to our experiments, performs on par with, and sometimes  
285 out-performs, other code developed directly for a specific data format.

## 286 4 System Architecture

287 The Visualizer software was designed with maximum modularity in mind, as a toolbox of generic  
288 interacting components, each encapsulating a particular functionality. While it is beyond the scope of  
289 the paper to describe each component of the software package, we provide references which describe  
290 these elsewhere and focus the discussion on those aspects that the user interacts with and are directly  
291 related to achieving the real-time, direct manipulation of data. The lower-level components of this  
292 architecture have been described previously (Kreylos et al., 2001), but have since been completely  
293 redesigned for better performance, and the higher-level components and the module system have been  
294 added. The overall architecture of the new component toolbox is shown in Figure 3.

295 While many of these individual components are not new to the visualization community, our contri-  
296 bution lies in integrating these pieces into a software package that is geared towards data exploration  
297 and is portable to a wide range of VR or desktop environments. Components fall into three basic  
298 categories: *Data representation*, *visualization algorithms*, and *visualization elements*. Visualizer uses  
299 the C++ template mechanism to combine concrete instantiations of all components required to vi-  
300 sualize a particular data format, and a *data file reader* required to load individual data set formats,  
301 into a *visualization module*. These visualization modules are packaged as external plug-ins, and loaded  
302 into the overall Visualizer application at run-time when a user requests loading a data file. A module  
303 advertises to the overall application the scalar and vector variables contained in the current data set,  
304 and the visualization algorithms that can be performed on it. Visualizer then creates a graphical user  
305 interface to allow users to select variables and algorithms and assign them to input device buttons.  
306 The result of executing a visualization algorithm on a data set is a visualization element, e.g., a vol-  
307 ume, a color-mapped slice or an isosurface. Elements are stored in a scene graph inside the Visualizer

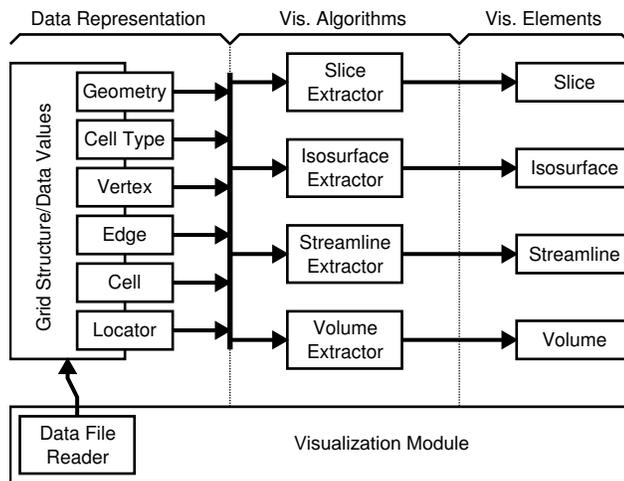


Fig. 3. Visualizer’s system architecture. Modules are plug-ins encapsulating the data structures and algorithms to visualize a particular data format, and are created by linking concrete instantiations of the underlying generic components.

308 application and can be toggled on/off and deleted individually.

309 The C++ template mechanism is very powerful for creating component architectures. As opposed to  
 310 run-time polymorphism, where descendants of the same base class can only differ in the implemen-  
 311 tation of virtual functions, templates allow one to additionally use different data types, supporting  
 312 more powerful abstractions (Alexandrescu, 2001). Furthermore, templates are instantiated and linked  
 313 at compile-time, allowing the compiler to perform full optimization on the generated code. As a result,  
 314 generic code often performs as well as specialized code, and sometimes better than specialized C code  
 315 due to the compiler’s ability to optimize across function calls (GCC Compiler, 2007; Alexandrescu,  
 316 2001). To combine the benefits of high performance and run-time polymorphism, our module archi-  
 317 tecture links sets of closely interacting components at compile-time into larger polymorphic modules  
 318 that only loosely interact with the overall application.

#### 319 4.1 Data Representation

320 The core component of all visualization modules is the representation of the visualized data set. Visu-  
 321 alizer currently supports regular (Cartesian), curvilinear (hexahedral) and unstructured (tetrahedral)  
 322 grid structures, commonly found in finite element simulations (Hughes, 2000). The interface between  
 323 data representations and visualization algorithms is implemented as a set of utility classes giving ac-  
 324 cess to the underlying geometry of a data set, i. e., the dimension and scalar type of its domain space,  
 325 the type of its cells, currently simplices or n-dimensional cuboids, and the vertices, edges, and cells  
 326 defining the data values and grid structure. A final accessor class, *Locator*, is a spatial iterator: it  
 327 makes it possible to query data values and local grid structure at arbitrary positions inside the data  
 328 set’s domain. Depending on the grid structure, data representation components contain acceleration  
 329 structures to query the neighborhood relationships between cells, and to support the interface to the  
 330 *Locator*.

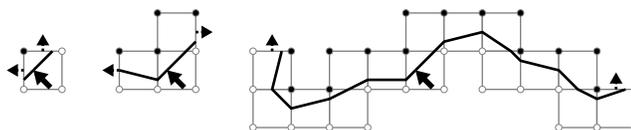


Fig. 4. Creation of a seeded isosurface. Extraction starts with the cell containing the Locator. After each cell is processed, the algorithm determines into which neighboring cells the isosurface extends, and adds those to the queue of pending cells. Processing the queue in order causes the isosurface to grow outwards from the cell containing the Locator. The black and white dots denote grid vertices whose value is above and below the isovalue (the interpolated data value at the Locator’s position), respectively.

## 331 4.2 Visualization Algorithms

332 Visualization algorithms create visualization elements such as slices and isosurfaces based on the grid  
 333 structure and data values of a data set, and the position/orientation of a Locator. Although Visualizer  
 334 contains “global” algorithms such as isosurfaces specified by isovalue and slices specified by position  
 335 and orientation, its user interface focuses on direct manipulation, i. e., the creation of elements based  
 336 only on a point/orientation of interest: this is a key feature that distinguishes Visualizer from other  
 337 VR software (Table 1). Visualizer currently supports color-mapped slices, isosurfaces, streamlines, and  
 338 volume rendering (Hansen and Johnson, 2004). In accordance with the direct manipulation approach,  
 339 and to provide more meaningful immediate feedback to users, most algorithms are *seeded* implemen-  
 340 tations (Meyer and Globus, 1993; Kreylos et al., 2001). As illustrated in Figure 4, a seeded algorithm  
 341 does not create visualization elements by processing an entire data set cell-by-cell, but instead starts  
 342 element creation from the cell containing the point of interest, and traverses all other cells containing  
 343 the same element radially outwards. This means that any intermediate results created by seeded algo-  
 344 rithms provide local information in an area around the point of interest, and allow a user to explore a  
 345 region of a data set by moving the point of interest while observing the change of the element’s shape  
 346 as it is dragged along (see movies). Once the user stops dragging, the partial element is created to  
 347 its full extent, or to the maximum number of graphics primitives the display system can render in its  
 348 allotted frame time (see movies).

349 The main benefit of a generic component architecture is that algorithms can be expressed independently  
 350 of grid format. For example, Visualizer contains only a single implementation of isosurfaces, which is  
 351 applied to all grid formats. By using the interfaces described in the previous section and listed in Table  
 352 2, the isosurface algorithm only contains the logic of how to create isosurface fragments inside a single  
 353 cell based on vertex values, how to traverse all cells containing the isosurface, and how to use timers  
 354 to satisfy real-time constraints. Any additional required information, such as triangulation case tables,  
 355 cell neighborhood information, and the formulas used to interpolate vertex positions/data values along  
 356 cell edges, are provided by the data representation interface classes.

357 Another benefit of a generic component architecture is the ability to provide specialized implementa-  
 358 tions of components. For example, there are many different ways to volume-render 3D data, and some  
 359 of the highest-performance ones only work on particular data types (Hansen and Johnson, 2004). In  
 360 these cases it is possible to provide special-case components, and the C++ compiler will use them  
 361 automatically when possible. For example, Visualizer’s generic volume rendering algorithm is based on  
 362 blending color-mapped slices (Reed et al., 1996); the specialization for regular (Cartesian) grids uses

363 hardware-assisted volume rendering based on 3D textures (Cabral et al., 1994) to achieve frame rates  
364 high enough for immersive visualization.

### 365 *4.3 Visualization Elements*

366 Visualization elements, such as color-mapped slices or isosurfaces, are produced by visualization algo-  
367 rithms, and stored in a scene graph (Wernecke, 1994) managed by the overall Visualizer application.  
368 Element components share lower-level implementations, such as triangulated surfaces optimized for  
369 high-performance rendering, and provide an interface for algorithms to create those in a streaming  
370 fashion. This additional separation of algorithms and their resulting data allows developers to opti-  
371 mize them separately. For example, changing the initial implementation of isosurfaces from unordered  
372 triangle sets to indexed triangle sets increased rendering performance substantially, and only required  
373 changing a single type definition inside the Isosurface component, and no changes in the Isosurface  
374 Extractor component. Once the superior performance of indexed triangle sets was established, we  
375 changed the Isosurface Extractor to generate indexed triangles internally, increasing extraction speed  
376 by a large factor. We expect that implementing even higher-performance surface representations will  
377 be not much more difficult. While such features are of no immediate interest to users, they allow devel-  
378 opers to more quickly and easily experiment with new algorithms or data structures, both to improve  
379 performance or to create new analysis tools. It is this flexibility that has enabled us to rapidly expand  
380 Visualizer for new scientific applications such as the ones described in Section 5.

### 381 *4.4 Visualization Modules*

382 A visualization module ties together all components required to visualize a particular data format,  
383 and a file reader to load concrete data sets from external storage. The actual code of a visualization  
384 module is usually very short. It only contains “glue code,” i. e., type definitions to describe the internal  
385 structure of the data and the required components, and the code to read grid structures and data  
386 values from an input file and store them in the data representation.

387 The module concept is the incorporation of an approach to data handling that differs from many other  
388 visualization applications. Many applications, including Tecplot and Vis5D, define a “native” data  
389 format, and users have to convert their data to this data format in a pre-processing step. Although these  
390 conversions are generally simple, having to keep several versions of the same data in several formats  
391 wastes storage space, and conversions can lose precision, especially since most interchange formats are  
392 plain ASCII tables. More importantly, conversion means that it becomes impossible or inefficient to  
393 directly stream intermediate results from a running simulation code into a visualization application to  
394 monitor the process of an ongoing simulation, and potentially even manipulate simulation state on-  
395 the-fly (Kreylos et al., 2002). Our ultimate goal for Visualizer is to have it used in such a context; hence  
396 we decided not to enforce native data formats for each basic grid structure, but to give programmers  
397 the ability to make the simulation’s data format native to Visualizer by coding a visualization module.  
398 From a user’s point of view, Visualizer does not have one native data format, but as many as there are  
399 visualization modules. Our approach is also different from providing file reader plug-ins, which convert

400 data file formats into an internal format. Instead, all data representation, visualization algorithm, and  
401 visualization element components related to a particular data format are compiled specifically for the  
402 data format, giving the compiler the option to optimize across component boundaries. We believe that  
403 our approach yields higher extraction and rendering performance.

#### 404 4.5 Overall System Architecture

405 The Visualizer application itself is responsible for managing all loaded visualization module plug-ins,  
406 all loaded data sets, the graphical user interface that lets users select variables and algorithms, and  
407 the scene graph of created visualization elements. Another important component is the *DataLocator*  
408 module responsible for translating input device interactions to extracting visualization elements, as  
409 explained in Section 3, and for displaying intermediate extraction results for real-time feedback. Addi-  
410 tionally, Visualizer contains modules to measure the position of and data value at arbitrary locations,  
411 to edit the color maps applied to all data variables individually, and to add interactive clipping planes  
412 (i.e., planes that remove all 3D content behind a 3D plane defined by the user’s input, to reveal the  
413 internal structure of visualization elements, or previously occluded elements) to the visualization.

#### 414 4.6 Tying It All Together

415 Judging by the descriptions provided in this section, it might seem that Visualizer is more of a pro-  
416 gramming toolkit for visualization software than an actual application aimed at end users. And this  
417 impression is partially true; our experience shows that VR visualization requires fine-tuned algorithms  
418 and data structures that sometimes depend on the particular data set to be visualized, and sometimes  
419 a particular scientific question requires custom analysis tools that need to be implemented at a low  
420 level to perform in real time. Visualizer’s component toolkit enables programmers to quickly add such  
421 custom algorithms, and experiment until their optimal implementation is found. Finally, reading a  
422 particular data set requires writing a data file reader, and the “glue” code that binds all required  
423 components into a visualization module.

424 However, from a user’s point of view, Visualizer is a complete application for visual exploration. If  
425 users happen to use a data format that is already supported by a visualization module, they can read  
426 it directly without the need for any scripting or programming; if there is no module, they can initially  
427 convert their data to a supported format in the same way they previously did for other visualization  
428 software, or find a programmer to write a custom module for their data. In our experience, this has  
429 not been a barrier for a wide range of datasets.

## 430 5 Evaluation

### 431 5.1 Visualizer Performance for Interactive Virtual Exploration

432 As Visualizer is designed for immersive VR environments, it is important to ask whether its imple-  
433 mentation satisfies the VR real-time constraints. To evaluate this, we measured its performance on  
434 the data set described in case 1 and used in the user study (see below and Figure 5), on a desktop  
435 PC with a 2.4 GHz AMD Athlon 64 X2 CPU, 1 GB of RAM, and an Nvidia Geforce 7800GS graphics  
436 card. The test data set is defined on a curvilinear hexahedral grid of  $271 \times 81 \times 201$  vertices, with two  
437 variables (temperature and viscosity) given for each vertex. The data set is stored in the native ASCII  
438 format written by the simulation code, and occupies 353.5 MB of disk space.

439 On loading the data set, Visualizer needed 12.4 s to parse the input file, convert all vertex positions from  
440 spherical to Cartesian coordinates, calculate the decadic logarithm of the viscosity values (viscosities are  
441 best visualized logarithmically), and create a kd-tree, a part of the internal representation of curvilinear  
442 grids containing all cell centers (Preparata and Shamos, 1993), that is later used to quickly find the  
443 cell containing a given position. Most of this time is spent parsing the ASCII input file (creating the  
444 kd-tree of 4.4 million vertices takes about 3 s); storing input data as binary files reduces load times  
445 substantially. Afterwards, we measured how long it takes to extract the isosurface shown in Figure 5, b),  
446 using smooth shading with vertex normal vectors computed as data value gradients. Creating a seeded  
447 isosurface from the center point of the feature shown in Figure 5, c), took 304 ms and generated  
448 339,722 triangles. For comparison, creating a global isosurface of the same isovalue took 744 ms and  
449 generated 339,854 triangles (the isosurface has a small disconnected component not extracted by the  
450 seeded algorithm). After extraction, Visualizer was able to render either isosurface at a frame rate of  
451 146.8 frames/second, or 49.9 million triangles per second. During dragging, the extraction algorithm  
452 was able to create about 100,000 triangles before it had to stop and display the intermediate result  
453 due to the 0.1 s time-out; in other words, it was able to visualize a large region of the isosurface around  
454 the point of interest in real time.

455 Performance is similar in immersive environments. Startup in our CAVE takes a few seconds longer  
456 since Visualizer itself and the input data set have to be replicated to all six cluster nodes, but isosurface  
457 extraction times are about the same. The rendering performance in the CAVE is about a factor of two  
458 lower, since all surfaces have to be rendered twice in each frame (once for the left eye and once for the  
459 right eye).

### 460 5.2 Scientific Applications Using Visualizer: Three Case Studies

461 One of the most difficult questions to address regarding 3D visualization is whether analyzing obser-  
462 vational or experimental data or computer simulation results in a 3D immersive environment actually  
463 leads to scientific understanding or results that would not have been found using more traditional  
464 methods on a desktop computer. While it is not possible to provide a definitive answer to this question  
465 for all scientific data sets, we present three examples of how using Visualizer in both immersive VR

466 and desktop environments has impacted our own research and led to scientific understanding that was  
467 missed or not possible using other software or methods.

### 468 *5.2.1 Assessing 3D Simulation Input for Subduction Dynamics Models*

469 The interaction between tectonic plates at the Earth’s surface and convection in the mantle often  
470 manifests in deformation such as mountain building or rifting over long periods of time (e.g., millions  
471 of years). On these time scales the deformation of tectonic plates and the mantle can be modeled  
472 as viscous flow to gain insight into how coupling between plates, the viscosity and density structure  
473 of the mantle, and crustal structure contributes to observed deformation (Billen and Gurnis, 2001;  
474 Billen et al., 2003). Numerical simulations of deformation related to plate tectonics often incorporate  
475 the geometry of structures such as plate boundaries, crustal terranes or subducted lithosphere (slabs)  
476 for a particular study region. While 2D cross sections of regional geometries can be relatively simple,  
477 i.e., gently sloping faults, and smoothly varying slab dip, in 3D space these same structures can vary  
478 rapidly in directions that are not orthogonal to the model mesh, making them challenging to represent  
479 on meshes of limited resolution required for simulations. In particular, the success of iterative solution  
480 methods used in finite element models are strongly dependent on the smoothness of the viscosity and  
481 temperature field defining the tectonic plates and plate boundaries. In addition, the model simulations  
482 take anywhere from three days to two weeks to run on a 64-processor beowulf cluster. Therefore,  
483 the ability to troubleshoot problems with the input model before running the simulation can save an  
484 enormous amount of time and money.

485 Coauthors Billen and Jadamec are using Visualizer to assess the appropriateness of input models for  
486 finite element simulations of crust and lithosphere deformation in southern Alaska, and to analyze the  
487 results of these simulations. Figure 5a–d shows the viscosity structure for a 3D model of the subducting  
488 Pacific plate beneath southern Alaska. The realistic 3D geometry of the subducted plate and plate  
489 boundary weak zone incorporated in this model is based on the seismicity within the subducting  
490 plate (Ratchkovski and Hansen, 2002; Page et al., 1989; Gudmundsson and Sambridge, 1998) and  
491 is unusual for tectonic simulations, which usually use simplified geometries. The viscosity structure  
492 depends on both the constructed thermal structure of the subducting Pacific plate and overriding North  
493 American plate, and the specification of the geometry, width, and weakening within the weak zone of  
494 the plate boundary. Before Visualizer was available, the thermal structure and weak zone structure were  
495 constructed and examined with multiple mesh-orthogonal slices using MATLAB. Because the large  
496 size of the data set (20 million mesh points), it was not possible to view isosurfaces of the individual  
497 input structures, or to overlay the structures to examine their alignment. In addition, due to the large  
498 amount of time required to generate and view all the slices, only a subset of mesh slices were viewed to  
499 assess the smoothness and appropriate superposition of the two input structures. However, from the  
500 examination of the individual data sets, it was concluded that the structures were correctly positioned  
501 relative to one-another and were appropriately smooth for input to the numerical simulation.

502 Following failure of the numerical simulation to converge to a solution, the output viscosity structure  
503 was viewed in a CAVE environment using the Visualizer software. Isosurfaces created for multiple  
504 isovalues obtained by dragging the wand through the data set immediately revealed grid-aliasing prob-  
505 lems (stair-stepped isosurfaces from the thermal structure) and unintended holes in and protrusions

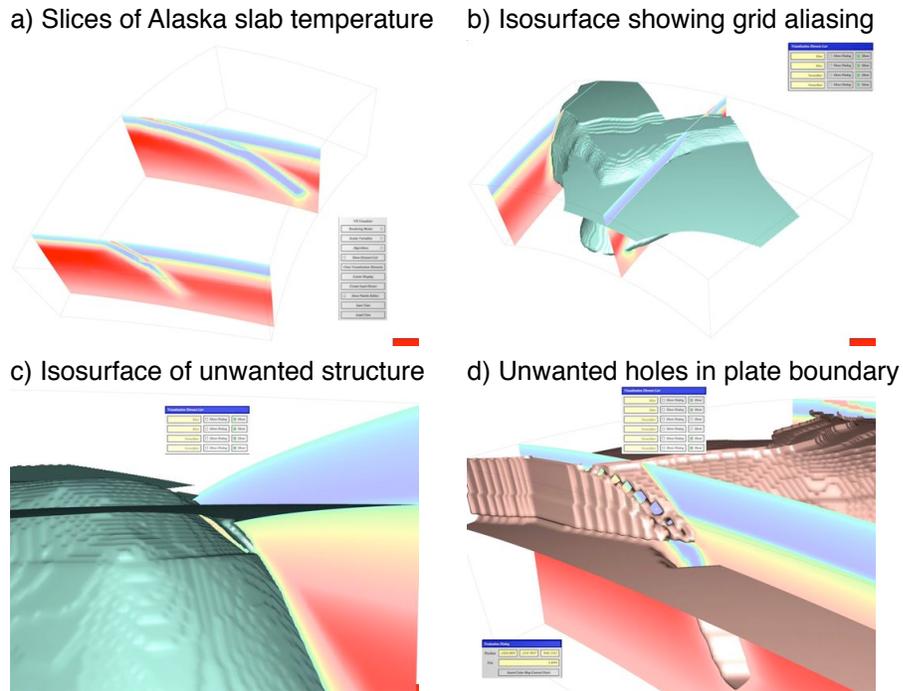


Fig. 5. Case study 1: Snapshots from input data set for finite element model of subduction (also used in user study). a) Color-mapped slices showing cross section of a subducted slab is used to locate initial problem features in a finite element model. b) Isosurface providing a 3D view of the subducting tectonic plate structure with stair-step aliasing on grid. c) Close-up view of a "problem feature" protruding from slab surface. d) Close-up view of a second problem feature, holes in the isosurface of the slab edge. See also Movies 1 and 2.

506 from the tectonic plate (Figure 5b–d). Dragging slices through the data set also illustrated the holes  
 507 and protrusions in these regions. These unintended features were located in regions where the radius  
 508 of curvature of the subducting plate was small and so changed rapidly with respect to the underlying  
 509 mesh. These features indicated that the failure of the model simulation to converge was a result of the  
 510 challenges in constructing the realistic 3D plate boundary zone geometry, rather than a limitation of  
 511 the iterative solver or finite element scheme. Based on analysis of the location and type of unintended  
 512 structures, a new method of smoothly defining the thermal structure and weak zone geometry was  
 513 implemented. Visualizer was used to quality-check the input data set before running the simulation.  
 514 The ability to drag isosurfaces that could be viewed in real time from multiple perspectives and to  
 515 drag slices through the data set for any orientation provided an efficient method of visually inspecting  
 516 the entire model input data set and make improvements before running the model. The newly con-  
 517 structed model input was then used for the simulation, which converged on a solution for the flow and  
 518 deformation associated with the subducting Pacific plate beneath Alaska (Figure 1c, d).

519 In this application, the interactivity built into Visualizer is the key advantage over other available  
 520 software. The ability to recognize the features of interest were similar on a desktop computer and in  
 521 the CAVE. However, both environments were used for different tasks. The immersive VR environment  
 522 was used when discussion of the causes of features and decisions on how to modify the input model were  
 523 made by more than one person. The desktop version was used to quickly check the result of incremental

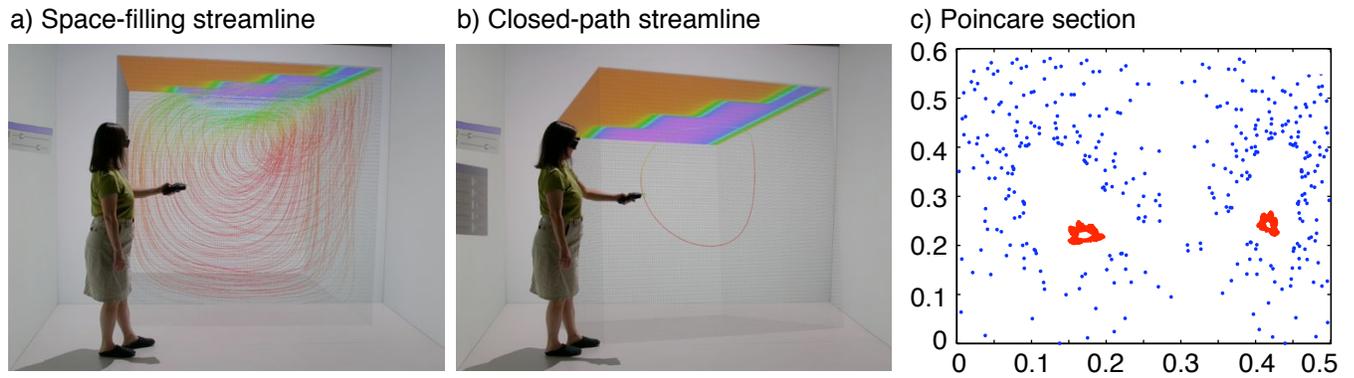


Fig. 6. Case study 2: Using the streamline visualization tool to investigate a 3D steady velocity field. (a) A particle path that appears space-filling. The plane shows the horizontal velocity near the top edge of the calculation; the spreading center and transform faults are visible. (b) Use of the streamline tool to explore the field reveals a contained region. This particle path has the same number of timesteps as the path in (a). (c) The Poincaré section shows crossing points for particle paths in the two regions shown in (a) and (b). The small area covered by the contained particle path (red) makes it difficult to find this feature without the use of Visualizer.

524 changes made to the procedure and methods used to make the input model. The flexibility of being  
 525 able to use Visualizer in either environment, while preserving the interactivity developed for use in an  
 526 immersive environment in the desktop environment, proved to be another key advantage over other  
 527 software.

### 528 5.2.2 Locating Closed Particle Paths in Chaotic 3D Flow Beneath Spreading Ridges

529 Convection in the mantle is responsible for mixing material that is recycled at subduction zones;  
 530 to interpret the different geochemical signatures of mantle-derived basalts one must understand the  
 531 extent and timescales of mantle mixing (Kellogg and Turcotte, 1990; Kellogg, 1992). Mixing in 2D has  
 532 been studied extensively, for example (Gurnis, 1986; Christensen, 1989; Kellogg, 1992), but studies of  
 533 mixing in 3D models of mantle flow have been limited by the few available methods for visualizing  
 534 and analyzing the flow in general and the resulting mixing in particular. Mixing in 2D incompressible  
 535 flows may be quite different from 3D mixing. For example, in steady-state flows in 2D space, the flow  
 536 is characterized by closed particle paths (Ottino, 1989); efficient mixing requires time-varying flow  
 537 (McKenzie, 1979; Olson et al., 1984) and chaotic particle paths can only develop in time-dependent  
 538 flows (Christensen, 1989; Kellogg and Stewart, 1991; Kellogg, 1992). In contrast, in steady-state 3D  
 539 flows with both a toroidal and poloidal component, chaotic particle paths have been found (Ferrachat  
 540 and Ricard, 1998; van Keken and Zhong, 1999). Moreover, turbulent mixing can coexist with regions  
 541 of laminar flow in which mixing is inefficient (Ferrachat and Ricard, 1998).

542 One method for finding nonchaotic regions embedded in a chaotic flow is based on constructing Poincaré  
 543 sections, in which the crossing points of a particle path are plotted on a plane bisecting the flow. The  
 544 nonchaotic paths will form a regular pattern of points restricted to a limited region of the plane. This  
 545 method requires a certain amount of serendipity in that the Poincaré plane must cross the non-chaotic  
 546 paths, and the particle paths selected must include the nonchaotic paths. In exploring a simplified

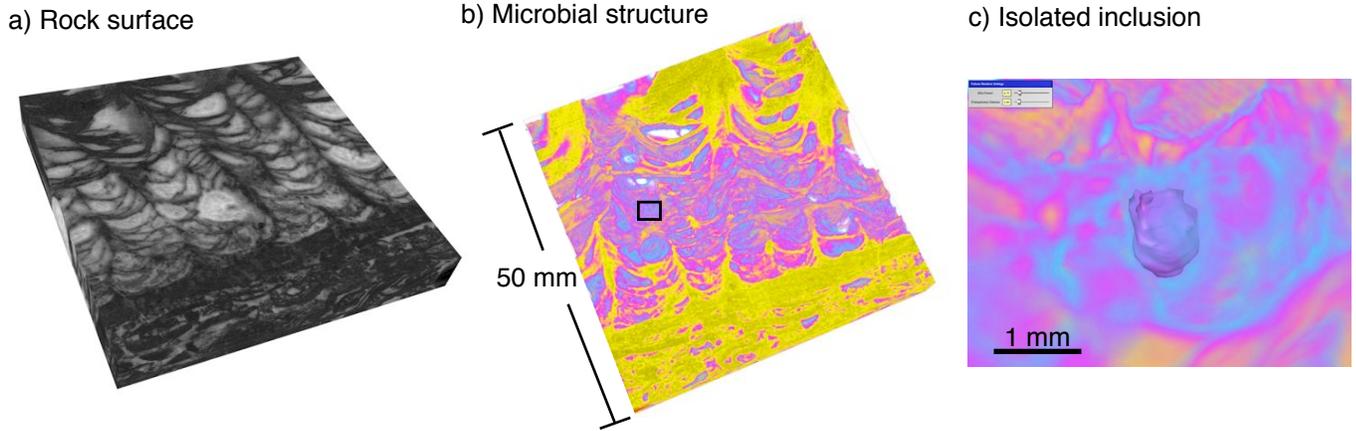


Fig. 7. Structure of fossil mats and biofilms in rocks. a) Reconstructed 3D volume of scanned thin sections of a rock. b) Color image of microbial structure in rock. c) Isolated inclusion of microbial material. See also Movie 3.

547 model of mantle flow beneath a spreading center with transform faults, co-author Kellogg found no  
 548 non-chaotic particle paths using the Poincaré method. However, after a few minutes of exploration  
 549 of the velocity data field using a streamline tool that interactively updates particle path stream lines  
 550 emanating from the wand, closed loop paths were discovered (Figure 6a,b). Starting at the point  
 551 specified by the user using the wand, Visualizer numerically integrates the velocity field to obtain a  
 552 particle path. (The user specifies the time-step used and number of steps in the integration.) These  
 553 paths occupy a small volume of space and are not single closed loop paths, which makes them difficult  
 554 to locate using traditional methods. Once the appropriate particle paths were identified, we were able  
 555 to use Poincaré sections to compare the structure to results from previous work (Figure 6c).

556 In this application, using Visualizer in an immersive environment provides both the interactivity needed  
 557 to thoroughly explore the 3D data set and the 3D viewing experience that allows the multiple streamline  
 558 paths to be viewed without the clutter of overlapping paths seen in the figure.

### 559 5.2.3 Exploration of Intricate Fossil Microbialites

560 The morphology of some microbial communities provides information about the organization and  
 561 behavior of the microbes forming the mats and biofilms. These structures are sometimes preserved  
 562 in ancient rocks and therefore are a record of early life on Earth. To use morphology to constrain  
 563 the early evolution of life, the structures in ancient rocks must be quantitatively compared to those  
 564 created by specific microbial processes and a precise understanding of the 3D geometry of intricate  
 565 structures is needed. This requires the reconstruction of the morphology of ancient structures and  
 566 the measurement of relevant features. Co-author Sumner is using Visualizer to characterize Archean  
 567 fenestrate microbialites (Sumner, 1997, 2000). The reconstruction of microbialite samples is done by  
 568 successively polishing 20  $\mu\text{m}$  off the surface of a sample and scanning each new surface. Scanned images  
 569 are aligned and assembled to define a reconstructed 3D volume (Figure 7a, Movie 3). Visualization  
 570 consists of rendering the volume and using a number of tools to manipulate views of the data. For  
 571 this application, the structure of the ancient microbial community is most effectively visualized by

572 rendering mineral components (white to light gray) fully transparent and microbial components (black  
573 to dark gray) in color with variably transparency (Figure 7b). Visualization of the volume in a non-  
574 stereo system provides significantly improved understanding of the structures over observing successive  
575 opaque images. Visualization in a 3D immersive environment provides even more substantial increases  
576 in understanding over non-stereo volume visualization, in addition to enabling precise measurement of  
577 features.

578 One significant advantage of stereo volume visualization is the ability to investigate data and see it in  
579 3D space while it is not moving. With non-stereo 3D visualization, one must continually manipulate the  
580 volume and use parallax to comprehend the full geometry of structures. This motion obscures details in  
581 the data; the user must remember the spatial relationships when viewing fine details in a static image,  
582 which is a significant challenge. For example, it is very difficult to evaluate whether a small microbial  
583 feature within a predominantly mineral-only areas is attached to a larger sheet of microbial structures  
584 or is fully isolated. In the absence of stereo rendering, one must move the image significantly to obtain  
585 parallax 3D vision and, if the feature is fairly isolated, detailed spatial relationships are only observable  
586 through slicing the data and removing geometrical information. Then the user must remember these  
587 relationships and observe the data at a high zoom to look for very small features such as isolated  
588 clumps of organic inclusions (Figure 7c, Movie 3). Rotations of the data must be found where multiple  
589 clumps occlude each other to obtain 3D spatial information. The need for parallax significantly limits  
590 the user's ability to understand the geometry. In contrast, in an immersive stereo environment, the user  
591 only needs to observe the volume at a high zoom, seeing the relationships among minute structures  
592 at any orientation and simultaneously seeing their relationships to larger structures with peripheral  
593 vision. The increased spatial understanding is obtained almost immediately and with much higher  
594 accuracy than is possible in a non-stereo system.

595 The insights from viewing the data can be extended to quantitative characterization of geometry  
596 within Visualizer. For our isolated clump example, the separation of structures could be due to either  
597 the primary growth geometry of the microbial community or the decay of organic matter after burial.  
598 Measurements such as the spacing between patches of preserved organic inclusions and the orientation  
599 of preserved patches are two very important constraints which cannot be obtained from 2D data and  
600 are inaccurate and extremely difficult to make without stereo rendering of the 3D data. In Visualizer,  
601 these measurements are easily made in the volume, both along and oblique to the original scanned  
602 images (Movie 3). With the precise locating of the pointer implemented in Visualizer, measurements  
603 can be made with an accuracy of the full resolution of the data set more quickly than the user can  
604 decide where to measure. The limits to obtaining quantitative information shift from the time spent  
605 manipulating data to obtain the measurements desired to the intellectual challenge of deciding which  
606 measurements best characterize the data.

### 607 *5.3 Assessing The User Experience*

608 Two of the major drawbacks of some software used in immersive environments are, first, that the  
609 software is difficult to learn and use, and second, that most software tools only work well on the  
610 desktop or in an immersive environment, but not in both (Table 1). Throughout the development of

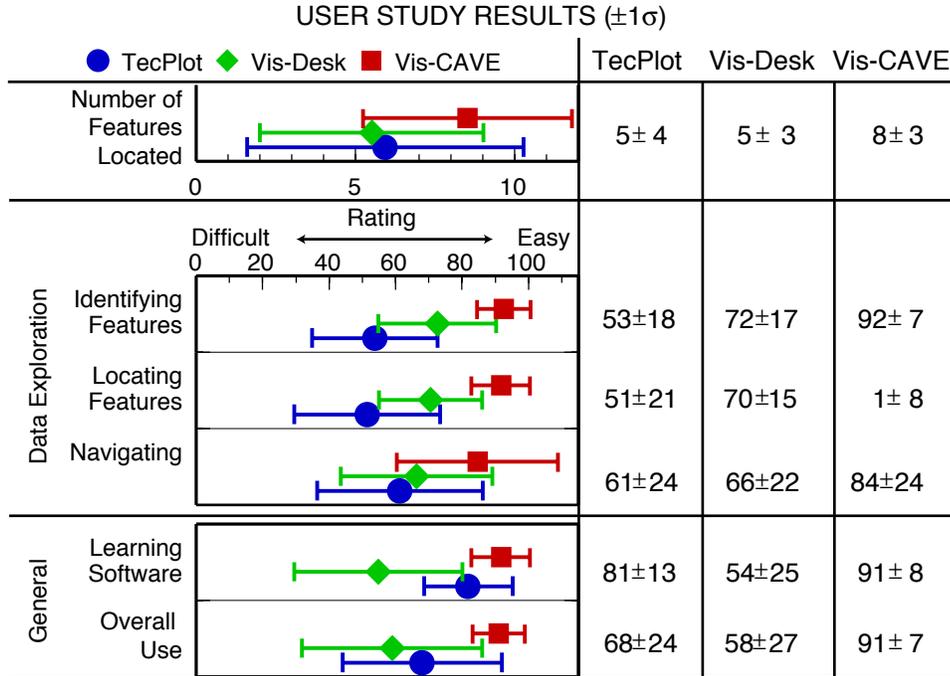


Fig. 8. User study results. Rating of data exploration (navigating, identifying and locating features) and general use (learning software and overall usability) displayed as the mean and standard deviation. Results show that Visualizer used in the CAVE made data exploration very easy and the software was easy to learn and use overall. Visualizer used on a desktop was also better for data exploration than Tecplot, but was more difficult to learn since the tool assignment process is somewhat cumbersome on the desktop.

611 Visualizer the goal has been to create a flexible, easy-to-use and intuitive tool for interactive, scientific  
 612 analysis of 3D volume data sets that can be used in multiple environments. However, the verification  
 613 of whether the software achieves this goal must be done by the scientists using the software. To  
 614 this end, we have conducted a user study aimed at assessing how well Visualizer aids researchers in  
 615 evaluating unknown data sets, by comparing it to Tecplot (TecPlot, 2006), described in Section 2, a  
 616 software package commonly used by geoscientists. Tecplot was chosen as a comparison because it has  
 617 a menu/button-driven interface that is similar to many other visualization programs. In the first part  
 618 of the study both visualization systems were compared in their native environments (Visualizer in a  
 619 CAVE and Tecplot on a desktop computer). In the second part of the study, Visualizer was also used  
 620 on a desktop computer and the results were compared to the those from the CAVE; Tecplot does not  
 621 run in VR environments.

### 622 5.3.1 User Study Format

623 In each software/environment setting, the study participants were asked to explore a data set and  
 624 to identify features that did not meet specified criteria: 1) features must be smooth and continuous,  
 625 without steps or faceted surfaces, and 2) features must be continuous, without holes or protruding  
 626 structures. The data used in all parts of the study is the model input of a subducting tectonic plate  
 627 beneath southern Alaska described in the case study on 3D numerical simulation (Figure 5). The tasks

628 performed by the study participants were based on the same steps used by geoscientists in analyzing  
629 the appropriateness of a model input data set for a FE model calculation.

630 Before beginning the prescribed tasks, the study participants were taught how to use the software  
631 in each environment using an idealized input data structure. Afterwards, the participants were then  
632 given 30 minutes to explore the target data set and instructed to write down the coordinates and data  
633 value for features they found that did not meet the specified criteria. After completing the analysis,  
634 the participants were asked about the tools within the software that they found most and least useful  
635 for navigating through the data set and identifying features. They were also asked to note any tasks  
636 that they found to be particularly easy or difficult to complete. Finally, after completing the tasks  
637 in all three software/environment settings, the participants rated the software on a scale of easy to  
638 difficult for the tasks of navigating, identifying features, locating features, learning the software, and  
639 overall use.

640 The study included 19 participants – eleven graduate students, five undergraduate students, and three  
641 faculty – engaged in geoscience study and/or research. Of the 19 participants, two had minimal previous  
642 experience using a CAVE and one had previously used Tecplot. Although none of the participants were  
643 experts on the scientific objectives related to this particular data set, all the participants were familiar  
644 with the general geologic problem.

### 645 *5.3.2 User Study Results*

646 The results of the user study, shown in Figure 8, demonstrate that the high level of interactivity pro-  
647 vided by Visualizer in the CAVE makes analysis of 3D volume data both easy and effective. Participant  
648 responses indicate that not only is data exploration (navigating, identifying and locating features) eas-  
649 ier to do in the CAVE than using Tecplot, Visualizer is also easier to learn how to use and easier to use  
650 overall. In addition, on average more features were located using Visualizer in the CAVE than using  
651 Tecplot or Visualizer on the desktop, although this part of the results is not conclusive and demands  
652 further investigation. The participants also found that data exploration is easier on the desktop using  
653 Visualizer than using Tecplot, but they also found it more difficult to learn how to use, which probably  
654 affected both their overall impression of the software and ability to locate features.

655 Participant feed-back on the individual software provided additional information on why Visualizer is  
656 easy to learn and use in the CAVE and more difficult to learn on the desktop. First, nine participants  
657 stated that they did not find any of the tasks to be difficult in the CAVE and found it particularly easy  
658 to identify and locate features. As one user reported, “the Visualizer-CAVE was by far the easiest to  
659 work with. All the features stood out very clearly and it was incredibly easy to navigate.” In contrast,  
660 13 participants stated that identifying and locating features in Tecplot was the most difficult task.  
661 We interpret this response to reflect both advantages of viewing the data set in a fully immersive  
662 environment and the intuitive design of the software.

663 Second, 13 users stated that assigning tools in Visualizer on the desktop was the most difficult task. In  
664 any environment, tool assignment in Visualizer requires first choosing what one would like the program  
665 to do (e. g., create isosurfaces) from the main menu and then assigning this action to to an input device  
666 button, e.g., a mouse button, by selecting a locator tool from the tool selection menu using the desired

667 button. On the desktop, however, two things make this process more cumbersome. First, buttons on the  
668 mouse are used to navigate (e. g., left button for rotating and right button for translating the data) and  
669 they are also used to create color-mapped slices or isosurfaces by using a modifier key on the keyboard  
670 (this caused confusion for new users who had to remember the button-key assignments). Second, the  
671 tool selection process on the desktop includes an extra step of creating a “virtual input device” to  
672 map 2D mouse positions into 3D model coordinates. User responses indicate that remembering the  
673 button-key combinations made tool assignment and use more difficult; however, they also stated that,  
674 once this was overcome, Visualizer was better for identifying and locating features. As one user stated,  
675 “the greatest difficulty is probably the initial complexity of click and key combination, but even in  
676 30 minutes I became pretty efficient with what I learned and I can see getting used to it very quickly.”  
677 Based on the responses and suggestions of the study participants, we plan to add an optional, fixed  
678 “tool bar” for tool assignment that can be used to introduce new users to Visualizer, but can be turned  
679 off once button-key combinations, which are faster to use, are learned.

680 The user study ratings and responses show that the interactivity provided by using Visualizer in a  
681 CAVE is intuitive and allows users to focus their attention on exploring the data set. In addition, they  
682 indicate that while interacting with a 3D data set in a 2D environment can be made effective in an  
683 interactive visualization system, it requires practice, while an immersive 3D VR environment provides  
684 immediate benefits by allowing the user to interact with data in a natural and intuitive manner. These  
685 results, combined with our experiences illustrated in the case studies above, suggest that immersive  
686 environments will become popular within scientific applications if software design meets the goals we  
687 addressed in Visualizer.

## 688 **6 Conclusions and Future Work**

689 We have presented new software for visualization of 3D gridded data sets, which has been designed for  
690 highly interactive, immersive 3D VR environments, but also achieves cross-system portability making  
691 it a powerful tool for visualization in the Geosciences. As an application aimed at immersive VR envi-  
692 ronments, Visualizer satisfies two real-time constraints: 1) it maintains a high frame rate upwards of  
693 30 Hz to create a realistic immersive experience, and 2) it provides real-time feedback (display of vi-  
694 sualization elements) to any user interaction within about 1/10s to enable interactivity. Interaction is  
695 further enhanced by following a direct manipulation approach across the entire range of functionality,  
696 from navigation to creation of visualization elements to quantitative analysis. At the software devel-  
697 opment level these constraints are met by using multithreaded programming, special algorithms such  
698 as seeded isosurfaces, advanced rendering using compressed geometry or multiresolution methods, and  
699 careful optimization of extraction and rendering algorithms. Meeting the real-time constraints for VR  
700 environments translates into an efficient and highly-interactive desktop application for very large data  
701 sets, which are often too large for real-time interaction using other software. Visualizer achieves this  
702 cross-system portability by being built on the Vrui development toolkit, being completely independent  
703 of the underlying VR environment and optimally matching interaction patterns to the capabilities of  
704 the underlying environment. While many of the optimization methods and visualization techniques  
705 used in Visualizer have been available in other desktop visualization software, our contribution lies in  
706 integrating these pieces into a software package that is designed for data exploration and analysis and

707 is portable to a wide range of VR and desktop environments.

708 The three case studies outlining how Visualizer has been used for Geoscience applications provide direct  
709 evidence of how Visualizer can enable discoveries or insight related to complex 3D gridded data sets.  
710 These case studies illustrate 1) how the interactivity speeds up analysis of the data leading to discovery  
711 of new behaviors (case study 2), 2) how the portability allows users to choose which environment best  
712 suits a particular task of data exploration and evaluation (case study 2), and 3) how viewing data with  
713 complex 3D morphology in a VR environment allows the user to recognize previously unseen features  
714 (case study 3). These examples also demonstrate how immersive stereo environments facilitate more  
715 detailed analysis of complex structures by eliminating the need to constantly move data to create  
716 parallax motion, and by providing zoomed-in views of data, while maintaining the perspective of larger  
717 spatial relationships with peripheral vision. Finally, the user study also provided valuable feedback on  
718 how further to improve Visualizer. We learned that effective exploration requires “transparent” user  
719 interfaces, such as intuitive navigation and “point and click” creation of visualization elements, and we  
720 will continue developing Visualizer, and the Vrui toolkit itself, to provide a more efficient, and easier  
721 to learn, user interface especially on the desktop.

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