## ECS20

Discussion 7: 02/20 to 02/26 2019

# Exercise 1

Let a, b, and c be three integers, with a non zero. Show that if  $a \mid bc$  and gcd(a,b) = 1, then  $a \mid c$ .

## Exercise 2

Let n be a natural number. We call s(n) the sum of its digits. Show that if s(n)=s(3n), then 9/n. (*Hint*: a number n is divisible by 3 if and only if s(n) is divisible by 3. Similarly, a number n is divisible by 9 if and only if s(n) is divisible by 9).

## Exercise 3

Let a be a non-zero integer. Show that if 2 does not divide a and 3 does not divide a, then  $24 \mid (a^2 + 23)$ .

## Exercise 4

Prove that for every three natural numbers x, y and z strictly greater than 1, there is some natural number larger than x, y and z that is not divisible by x, y or z.