



Last time

- Feature-based alignment
 - 2D transformations
 - Affine fit
 - RANSAC



































RANSAC: General form

RANSAC loop:

Slide credit: Kristen Grauman

- 1. Randomly select a *seed group* of points on which to base transformation estimate (e.g., a group of matches)
- 2. Compute transformation from seed group
- 3. Find inliers to this transformation
- 4. If the number of inliers is sufficiently large, re-compute estimate of transformation on all of the inliers

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Keep the transformation with the largest number of inliers











RANSAC pros and cons

- Pros
 - Simple and general
 - Applicable to many different problems
 - Often works well in practice
- Cons
 - Lots of parameters to tune
 - Doesn't work well for low inlier ratios (too many iterations, or can fail completely)

Lana Lazebnik

Today

- Image mosaics
 - Fitting a 2D transformationHomography
 - 2D image warping
 - Computing an image mosaic

HP frames commercial

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• <u>http://www.youtube.com/watch?v=2RPI5vPEo</u> <u>Qk</u>









How to stitch together a panorama (a.k.a. mosaic)?

- Basic Procedure
 - Take a sequence of images from the same position
 Rotate the camera about its optical center
 - Compute transformation between second image and first
 - Transform the second image to overlap with the first
 - Blend the two together to create a mosaic
 - (If there are more images, repeat)
- ...but wait, why should this work at all?
 - What about the 3D geometry of the scene?
 - Why aren't we using it?

23 Source: Steve Sei

























Why do we need homogeneous coordinates? • represent points at infinity, homographies, perspective projection, multi-view relationships

What is the geometric intuition?

a point in the image is a *ray* in projective space

- all points on the ray are equivalent: $(x, y, 1) \cong (sx, sy, s)$



















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- RANSAC for robust fitting – Lines, translation
- Image mosaics
 - Fitting a 2D transformationHomography
 - 2D image warping
 - Computing an image mosaic

























Recap: How to stitch together a panorama (a.k.a. mosaic)?

Basic Procedure

- Take a sequence of images from the same position
 Rotate the camera about its optical center
- Compute transformation (homography) between second image and first using corresponding points.
- Transform the second image to overlap with the first.
- Blend the two together to create a mosaic.
- (If there are more images, repeat)

43 Source: Steve Seitz









































RANSAC for estimating • RANSAC loop:

- 1. Select four feature pairs (at random)
- 2. Compute homography H (exact)
- 3. Compute *inliers* where $SSD(p_i)$, $Hp_i < \varepsilon$
- 4. Keep largest set of inliers
- 5. Re-compute least-squares H estimate on all of the inliers

55 Slide credit: St











- Verity transformation (search for other matches consistent with *T*) source: L Lazebni



- Verify transformation (search for other
 - matches consistent with T) Source: L. Lazebr

Summary: alignment & warping

- Write **2d transformations** as matrix-vector multiplication (including translation when we use homogeneous coordinates)
- Fitting transformations: solve for unknown parameters given corresponding points from two views (affine, projective (homography)).
- Perform image warping (inverse)
- **Mosaics**: uses homography and image warping to merge views taken from same center of projection.

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Slide credit: Kristen Grauman



