

Goal: interest operator repeatability

- We want to detect (at least some of) the same points in both images.



No chance to find true matches!

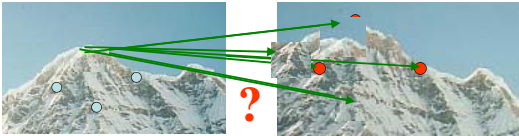
- Yet we have to be able to run the detection procedure *independently* per image.

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Goal: descriptor distinctiveness

- We want to be able to reliably determine which point goes with which.



- Must provide some invariance to geometric and photometric differences between the two views.

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Local features: main components

- 1) Detection: Identify the interest points



- 2) Description: Extract vector feature descriptor surrounding each interest point.

- 3) Matching: Determine correspondence between descriptors in two views

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Recall: Corners as distinctive interest points

$$M = \sum \begin{bmatrix} I_x I_x & I_x I_y \\ I_x I_y & I_y I_y \end{bmatrix}$$

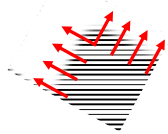
2 x 2 matrix of image derivatives (averaged in neighborhood of a point).



Notation: $I_x \leftrightarrow \frac{\partial I}{\partial x}$ $I_y \leftrightarrow \frac{\partial I}{\partial y}$ $I_x I_y \leftrightarrow \frac{\partial I}{\partial x} \frac{\partial I}{\partial y}$

Recall: Corners as distinctive interest points

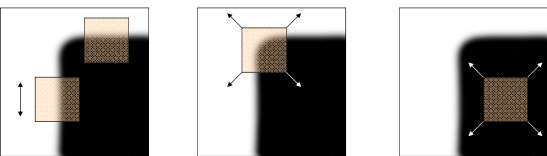
Since M is symmetric, we have $M = X \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} X^T$
(Eigenvalue decomposition)



$$Mx_i = \lambda_i x_i$$

The *eigenvalues* of M reveal the amount of intensity change in the two principal orthogonal gradient directions in the window.

Recall: Corners as distinctive interest points



"edge":
 $\lambda_1 \gg \lambda_2$
 $\lambda_2 \gg \lambda_1$

"corner":
 λ_1 and λ_2 are large,
 $\lambda_1 \sim \lambda_2$

"flat" region
 λ_1 and λ_2 are small;

One way to score the cornerness:

$$f = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$$

Harris corner detector

- 1) Compute M matrix for image window surrounding each pixel to get its *cornerness* score.
- 2) Find points with large corner response ($f >$ threshold)
- 3) Take the points of local maxima, i.e., perform non-maximum suppression

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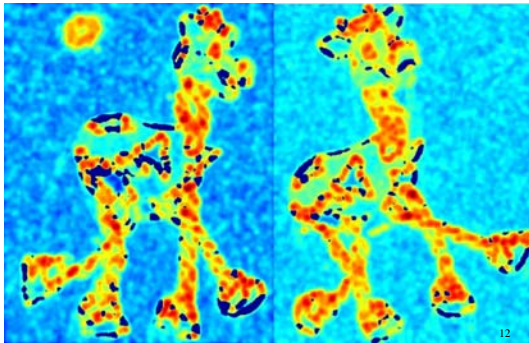
Harris Detector: Steps



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Harris Detector: Steps

Compute corner response f



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Harris Detector: Steps

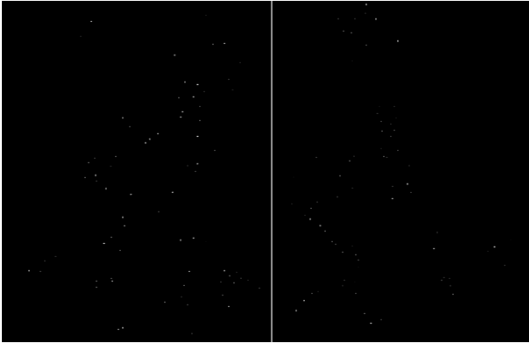
Find points with large corner response: $f > \text{threshold}$



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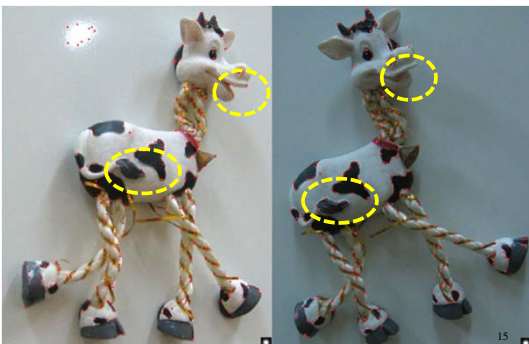
Harris Detector: Steps

Take only the points of local maxima of f




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Harris Detector: Steps



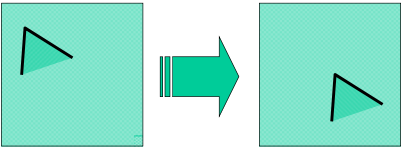
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Properties of the Harris corner detector
Rotation invariant? Yes



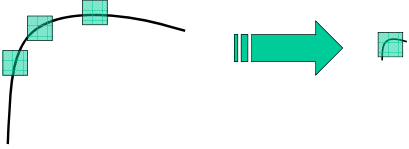
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Properties of the Harris corner detector
Rotation invariant? Yes
Translation invariant? Yes



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Properties of the Harris corner detector
Rotation invariant? Yes
Translation invariant? Yes
Scale invariant? No



All points will be classified as edges Corner !

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Scale invariant interest points

How can we independently select interest points in each image, such that the detections are repeatable across different scales?



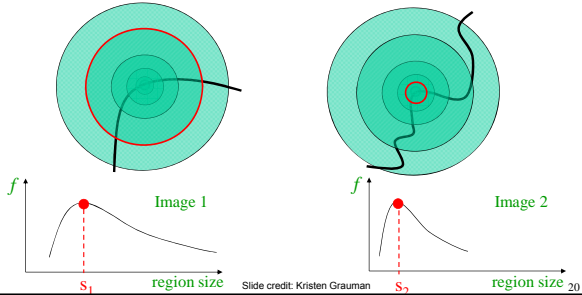
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Automatic scale selection

Intuition:

- Find scale that gives local maxima of some function f in both position and scale.



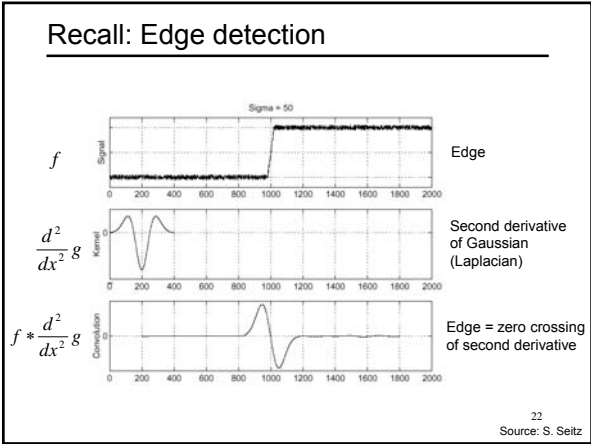
Slide credit: Kristen Grauman

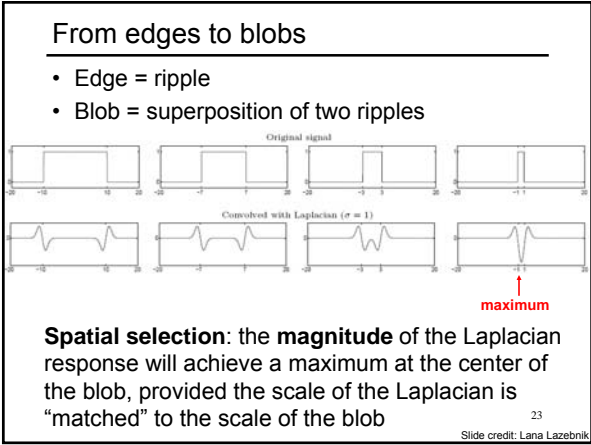
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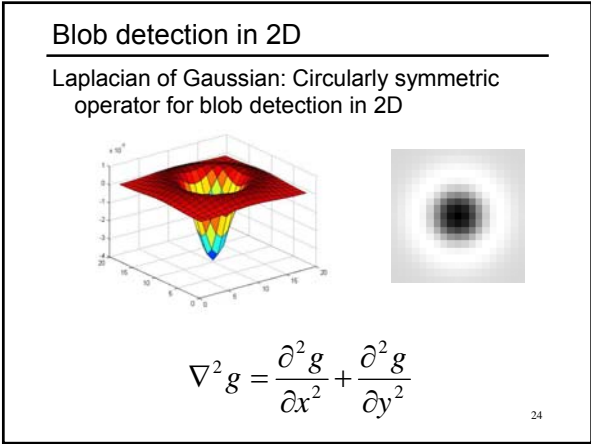
What can be the “signature” function?

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Blob detection in 2D: scale selection

Laplacian-of-Gaussian = "blob" detector $\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$

filter scales

img1 img2 img3

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Bastian Leibe

Blob detection in 2D

We define the *characteristic scale* as the scale that produces peak of Laplacian response

characteristic scale

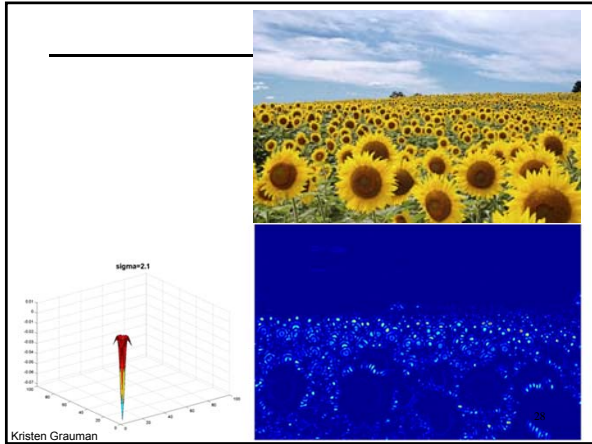
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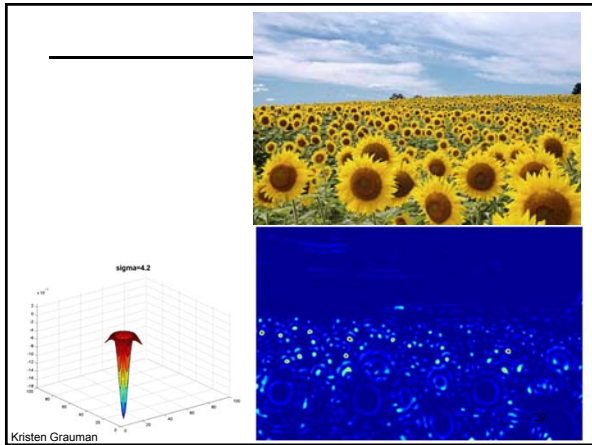
Slide credit: Lana Lazebnik

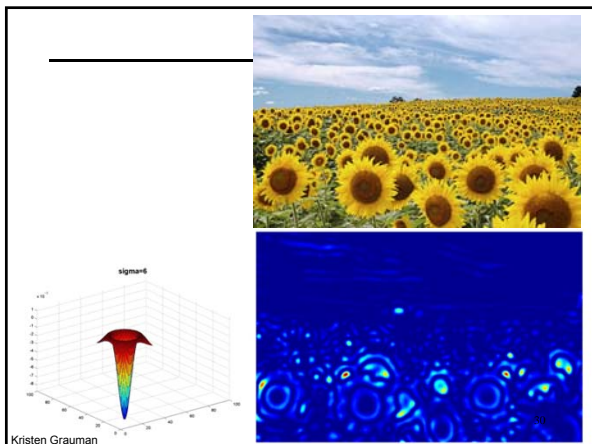
Example

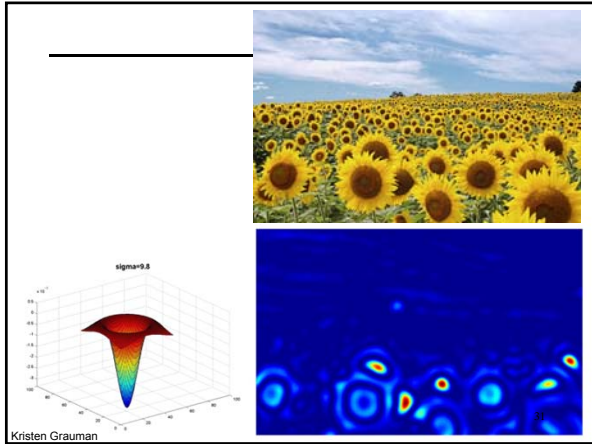
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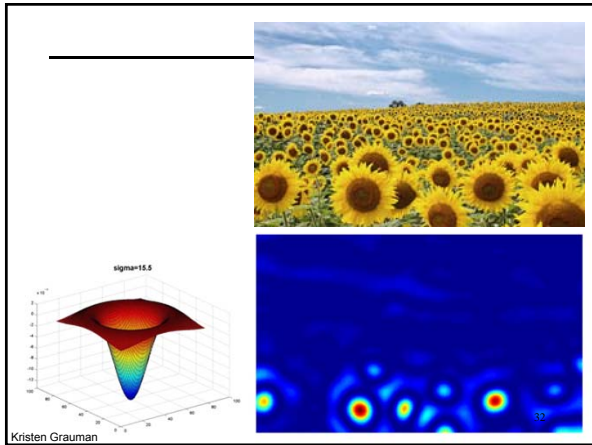
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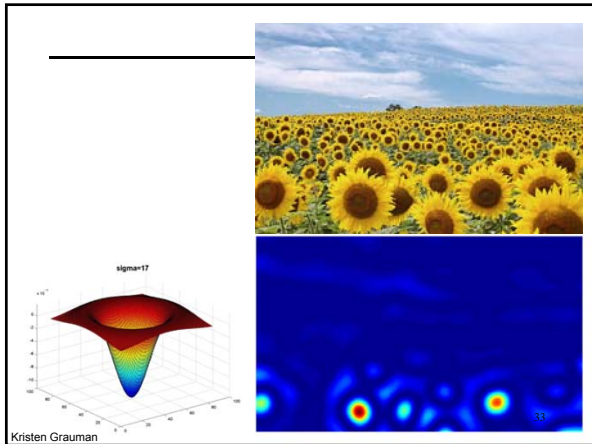






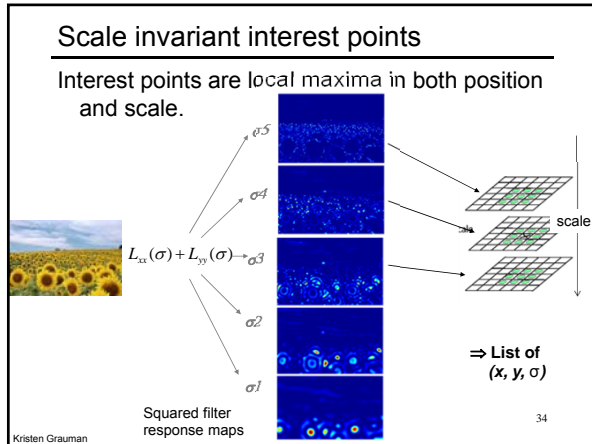






Scale invariant interest points

Interest points are local maxima in both position and scale.



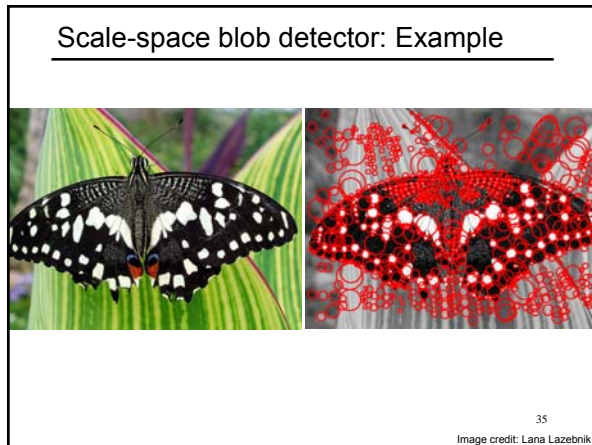
$L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$

Squared filter response maps

\Rightarrow List of (x, y, σ)

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Scale-space blob detector: Example



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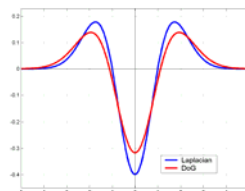
Image credit: Lana Lazebnik

Technical detail

We can approximate the Laplacian with a difference of Gaussians; more efficient to implement.

$L = \sigma^2 (G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$
(Laplacian)

$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$
(Difference of Gaussians)



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Local features: main components

1) Detection: Identify the interest points

2) Description: Extract vector feature descriptor surrounding each interest point.



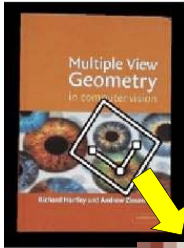
$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$

3) Matching: Determine correspondence between descriptors in two views

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Slide credit: Kristen Grauman

Geometric transformations



e.g. scale, translation, rotation₃₈

Slide credit: Kristen Grauman

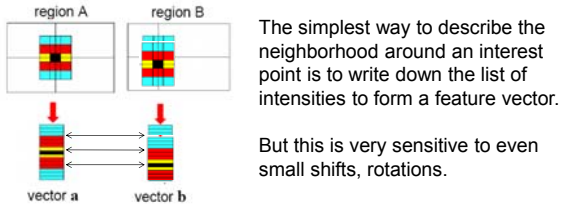
Photometric transformations



Figure from T. Tuytelaars ECCV 2006 tutorial

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Raw patches as local descriptors

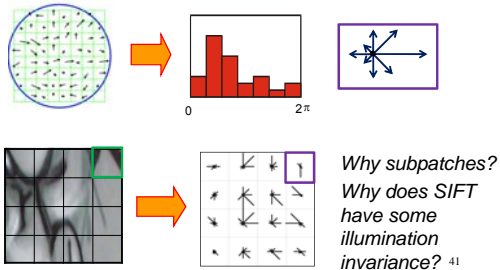


Slide credit: Kristen Grauman

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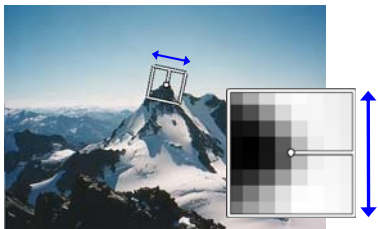
SIFT descriptor [Lowe 2004]

Use histograms to bin pixels within sub-patches according to their orientation.



Slide credit: Kristen Grauman

Making descriptor rotation invariant



- Rotate patch according to its dominant gradient orientation
- This puts the patches into a canonical orientation.

Image from Matthew Brown

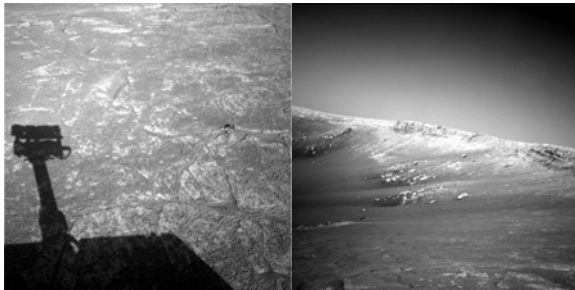
SIFT descriptor [Lowe 2004]

- Robust matching technique
 - Can handle changes in viewpoint
 - Up to about 60 degree out of plane rotation
 - Can handle significant changes in illumination
 - Sometimes even day vs. night (below)
- Fast and efficient—can run in real time
- Lots of code available
 - http://people.csail.mit.edu/abertladypack/wiki/index.php/Known_Implementations_of_SIFT



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Steve Seitz

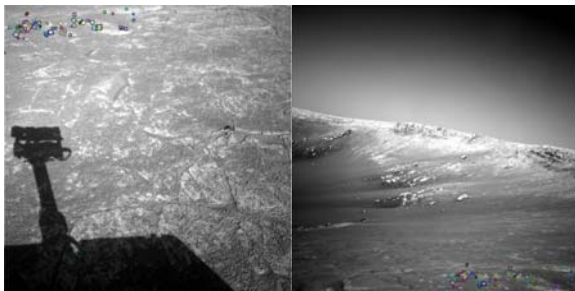
Example



NASA Mars Rover images

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Example



NASA Mars Rover images with SIFT feature matches
Figure by Noah Snavely

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SIFT descriptor properties

Invariant to

- Scale
- Rotation

Partially invariant to

- Illumination changes
- Camera viewpoint
- Occlusion, clutter

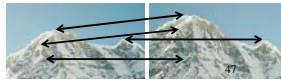
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Slide credit: Kristen Grauman

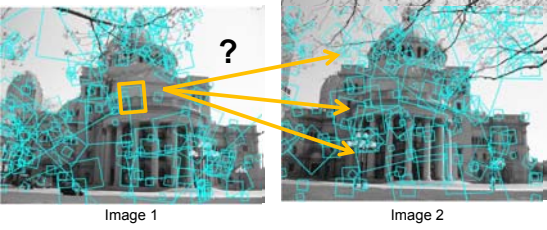
Matching local features



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Matching local features

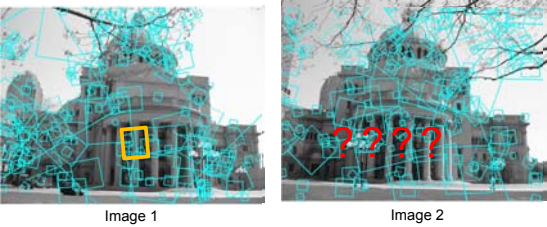


To generate **candidate matches**, find patches that have the most similar appearance (e.g., lowest SSD)
 Simplest approach: compare them all, take the closest (or closest k, or within a thresholded distance)

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Ambiguous matches



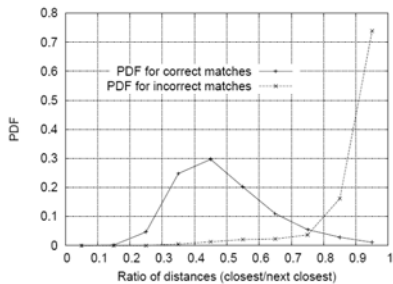
To add robustness to matching, can consider **ratio**:
 distance to best match / distance to second best match
 If low, first match looks good.
 If high, could be ambiguous match.

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Matching SIFT Descriptors

Nearest neighbor (Euclidean distance)
 Threshold ratio of nearest to 2nd nearest descriptor

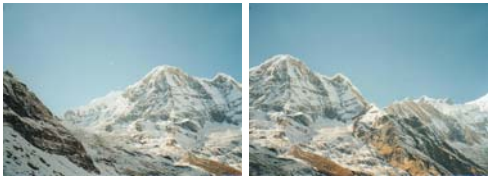


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Lowé IJCV 2004

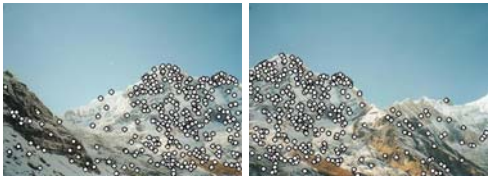
Recap: robust feature-based alignment



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Source: L. Lazebnik

Recap: robust feature-based alignment



- Extract features

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Source: L. Lazebnik

Recap: robust feature-based alignment

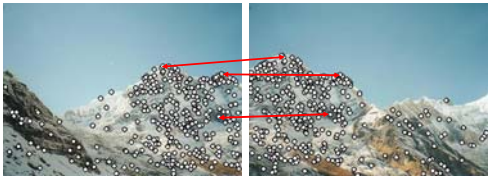


- Extract features
- Compute *putative matches*

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Source: L. Lazebnik

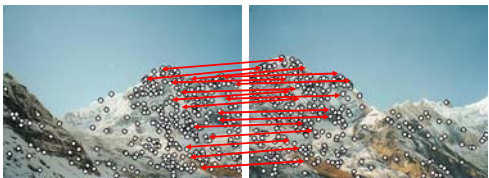
Recap: robust feature-based alignment



- Extract features
- Compute *putative matches*
- Loop:
 - Hypothesize transformation T (small group of putative matches that are related by T)

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Source: L. Lazebnik

Recap: robust feature-based alignment



- Extract features
- Compute *putative matches*
- Loop:
 - Hypothesize transformation T (small group of putative matches that are related by T)
 - Verify transformation (search for other matches consistent with T)

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Source: L. Lazebnik

Recap: robust feature-based alignment



- Extract features
- Compute *putative matches*
- Loop:
 - Hypothesize transformation T (small group of putative matches that are related by T)
 - Verify transformation (search for other matches consistent with T)

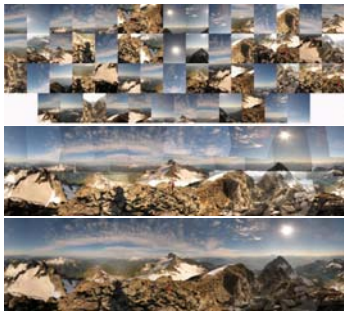
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Source: L. Lazebnik

Applications of local invariant features

- Wide baseline stereo
- Motion tracking
- Panoramas
- 3D reconstruction
- Recognition (better for instance matching)
- ...

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Automatic mosaicing



AutoStitch

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Wide baseline stereo



[Image from T. Tuytelaars ECCV 2006 tutorial]

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Recognition of specific objects, scenes



Schmid and Mohr 1997



Sivic and Zisserman, 2003



Rothganger et al. 2003



Lowe 2002

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Summary

Interest point detection

- Harris corner detector
- Laplacian of Gaussian, automatic scale selection

Invariant descriptors

- Rotation according to dominant gradient direction
- Histograms for robustness to small shifts and translations (SIFT descriptor)

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Questions?

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